

Waddle

Always-Canonical Intermediate Representation

Eric Fritz

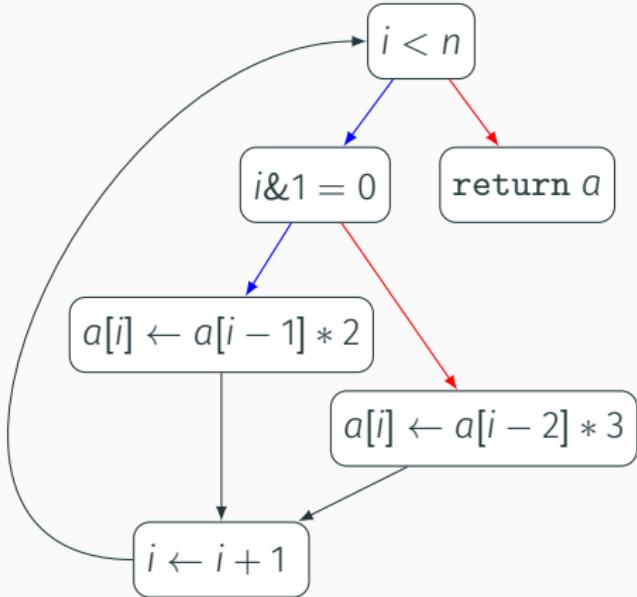
August 4, 2016

University of Wisconsin – Milwaukee



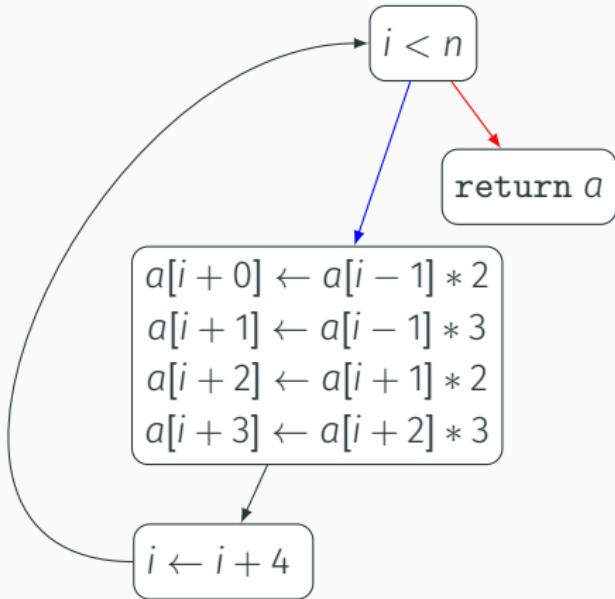
10,000 Foot View

```
1 while  $i < n$  do
2   if  $i \& 1 = 0$  then
3      $a[i] \leftarrow a[i - 1] * 2$ 
4   else
5      $a[i] \leftarrow a[i - 2] * 3$ 
6   end
7    $i \leftarrow i + 1$ 
8 end
9 return  $a$ 
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10,000 Foot View

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10,000 Foot View - LLVM 2.9 -O2 Passes

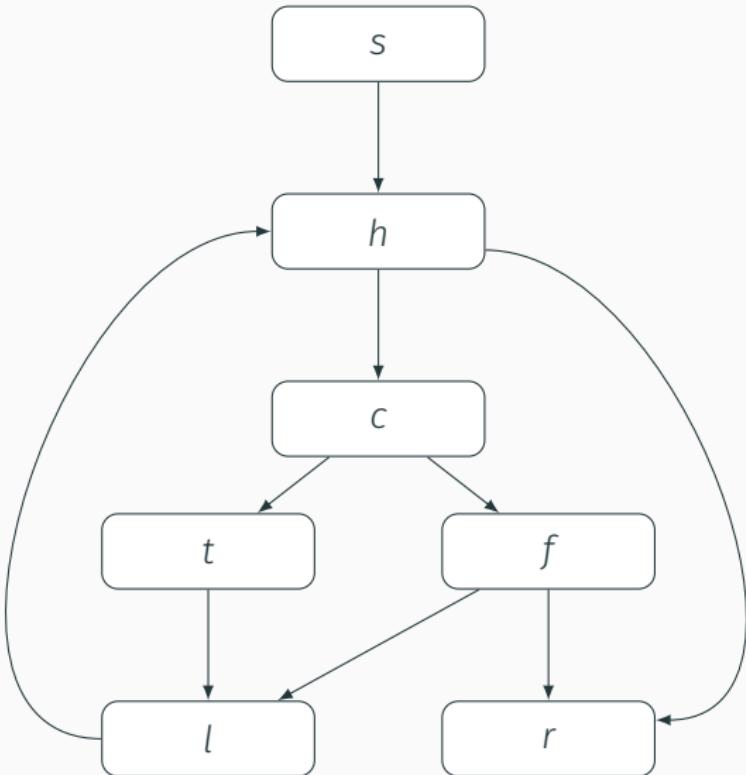
1. no/tb/basic-aa	20. reassociate	41. sccp	61. early-cse	80. loop-idiom
2. domtree	21. domtree	42. lazy-value-info	62. simplify-libcalls	81. loop-deletion
3. verify	22. loops	43. jump-threading	63. lazy-value-info	82. loop-unroll
4. lowersetjmp	23. loop-simplify	44. domtree	64. jump-threading	83. memdep
5. globalopt	24. lcssa	45. memdep	65. tailcallelim	84. gvn
6. ipsccp	25. loop-rotate	46. dse	66. reassociate	85. memdep
7. deadargelim	26. licm	47. adce	67. domtree	86. memcpyopt
8. basiccg	28. loop-unswitch	48. strip-dead-prototypes	68. loops	87. sccp
9. prune-eh	29. scalar-evolution	49. deadtypeelim	69. loop-simplify	88. lazy-value-info
10. inline	30. loop-simplify	50. globaldce	70. lcssa	89. jump-threading
11. functionattrs	31. lcssa	51. constmerge	71. loop-rotate	90. domtree
12. argpromotion	32. iv-users	52. globalopt	72. licm	91. memdep
13. scalarrepl-ssa	33. indvars	53. ipsccp	73. lcssa	92. dse
14. domtree	34. loop-idiom	54. deadargelim	74. loop-unswitch	93. adce
15. early-cse	35. loop-deletion	55. basiccg	75. scalar-evolution	94. strip-dead-prototypes
16. simplify-libcalls	36. loop-unroll	56. prune-eh	76. loop-simplify	95. deadtypeelim
17. lazy-value-info	37. memdep	57. inline	77. lcssa	96. constmerge
18. jump-threading	38. gvn	58. functionattrs	78. iv-users	97. domtree
19. tailcallelim	39. memdep	59. scalarrepl-ssa	79. indvars	98. verify
	40. memcpyopt	60. domtree		

Structure of Talk

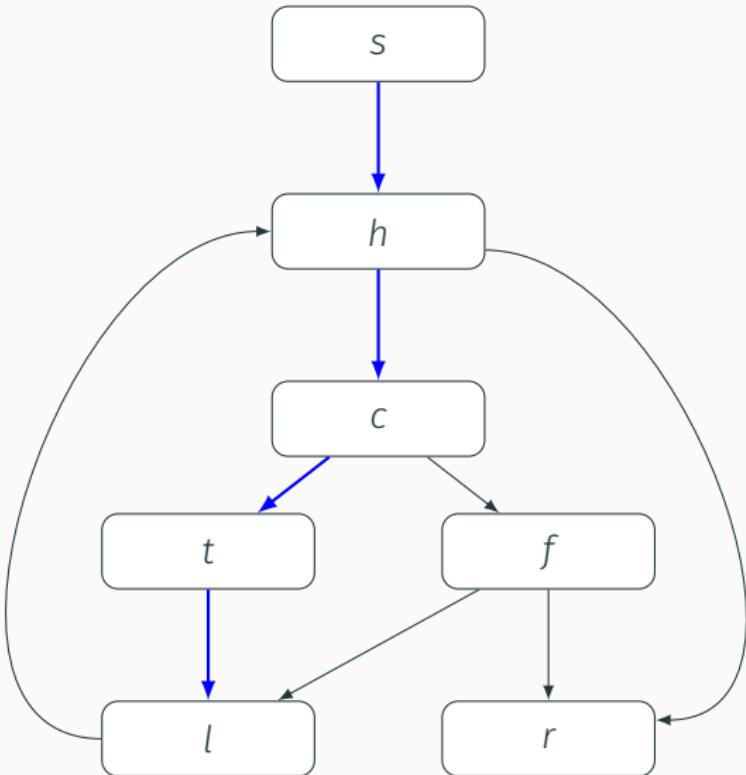
1. Auxiliary Structures, IRs
2. Motivation
3. SSA Reconstruction
4. Dominator Tree Reconstruction
5. Canonical Form Preservation
6. Tasklist

Auxiliary Structures, IRs

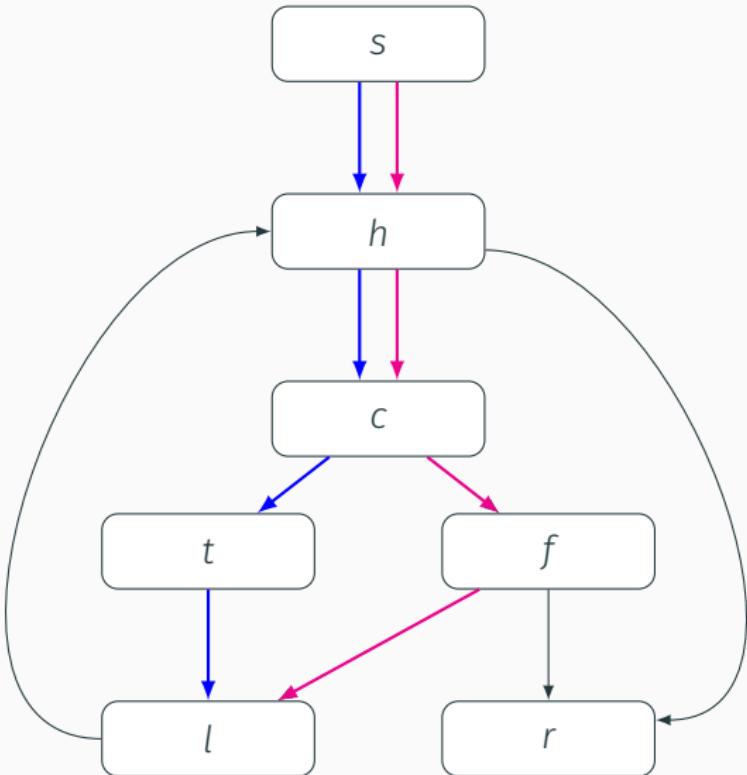
Domination



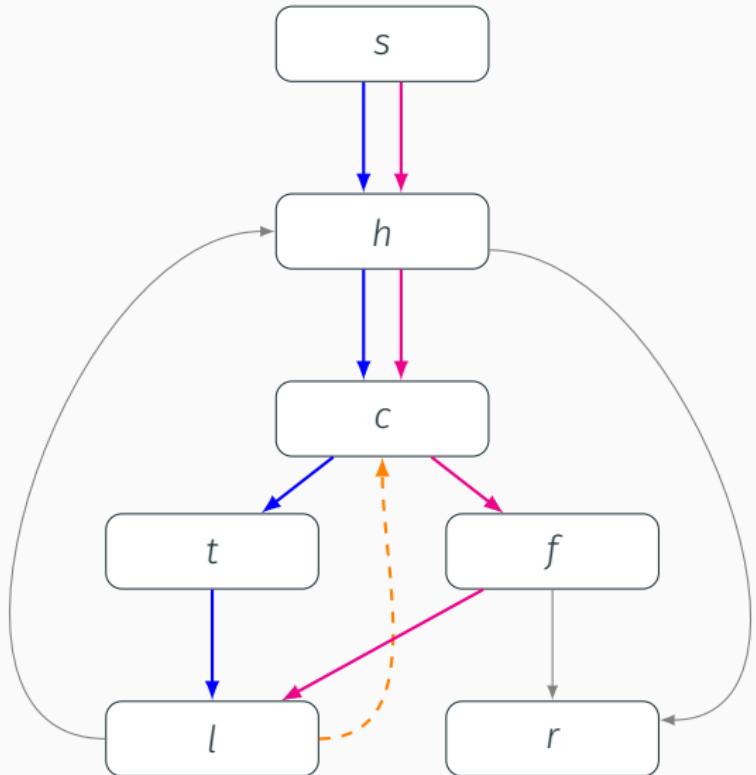
Domination



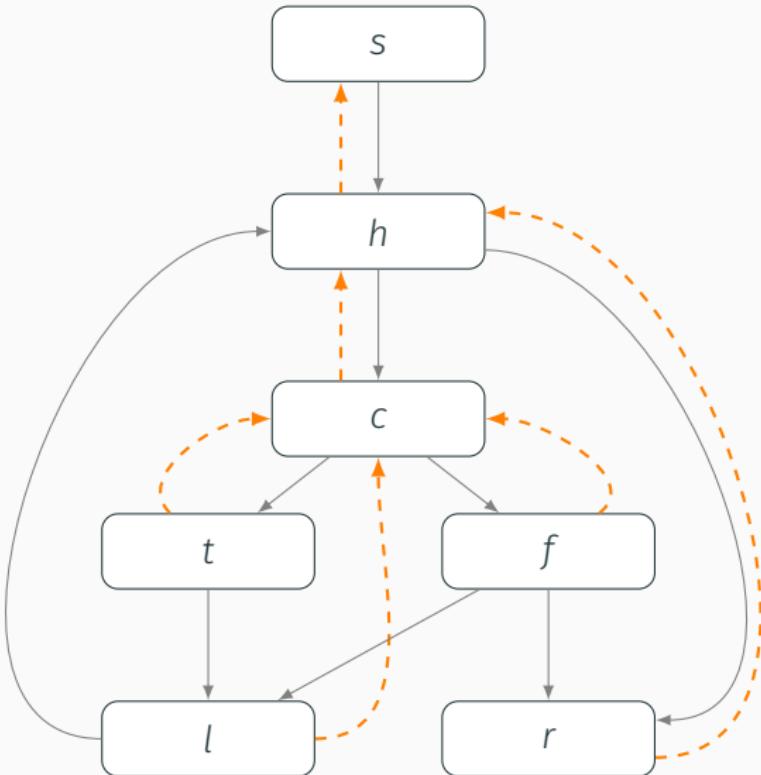
Domination



Domination



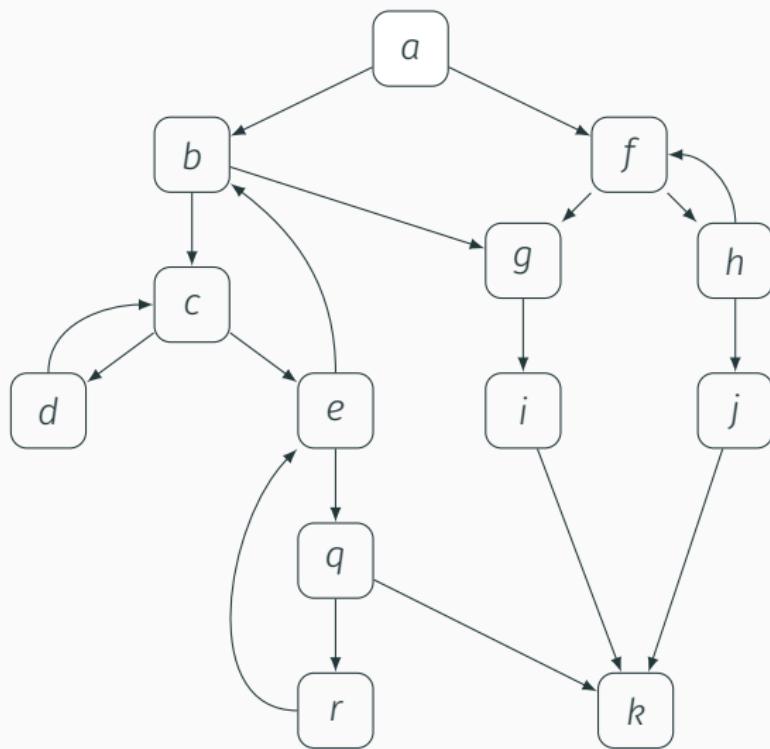
Domination



Domination - An (Extremely) Condensed History

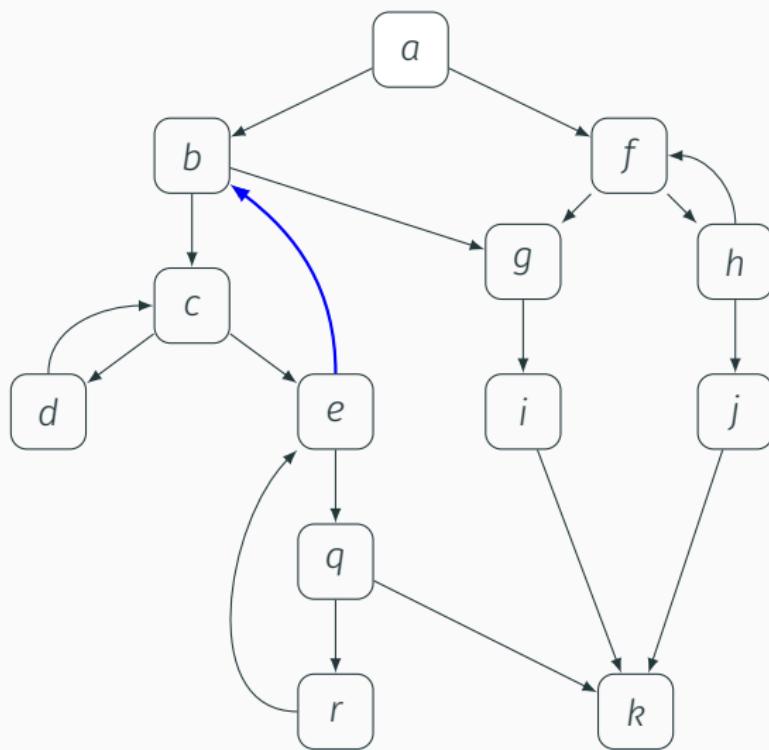
- Purdom-Moore, 1972
- Lengauer-Tarjan, 1979
- Buschbaum, 1998
- Cooper, 2001
- Georgiadis, 2005

Loops & Loop Nesting Forest



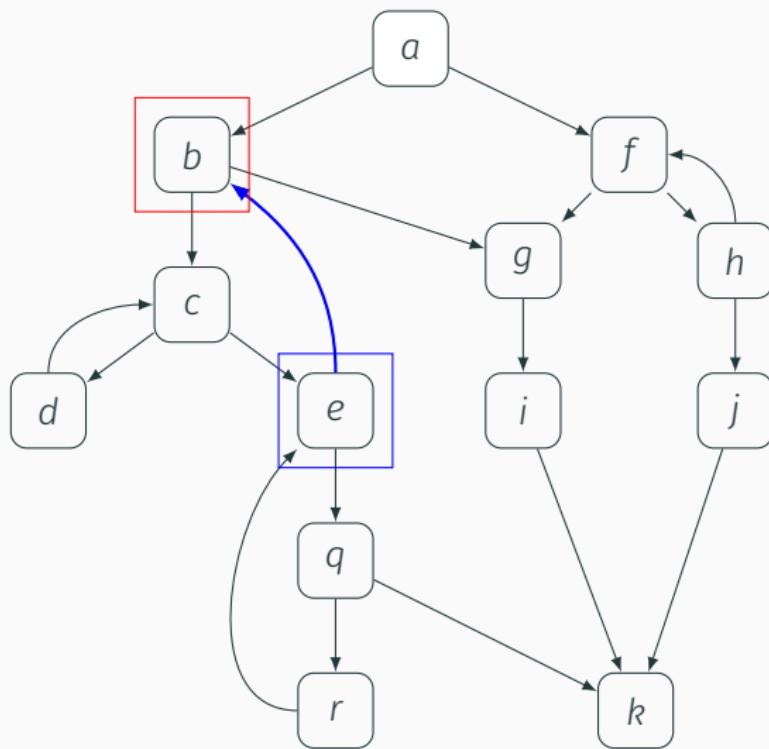
Loops & Loop Nesting Forest

(1) Identify Backedge



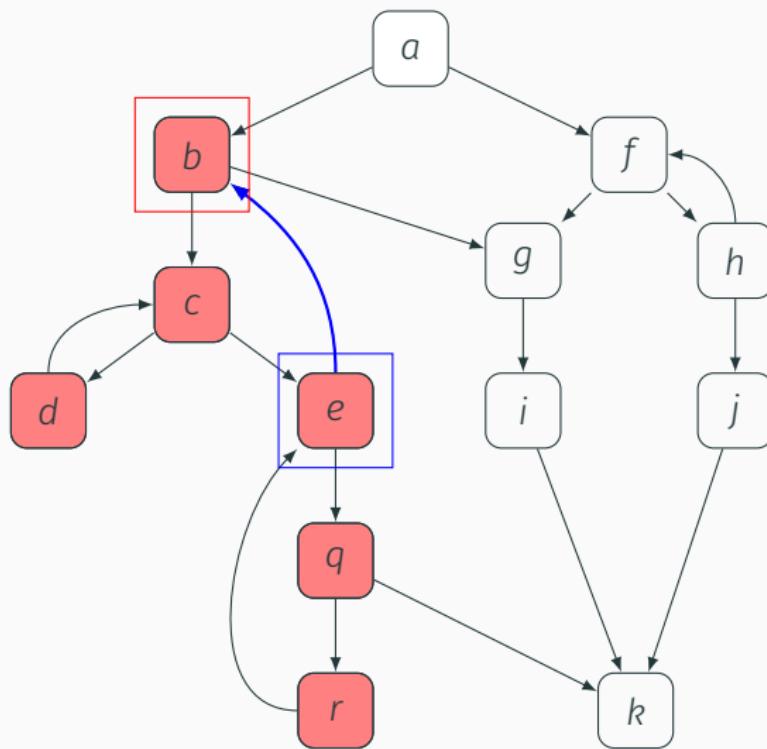
Loops & Loop Nesting Forest

(2) Identify Header



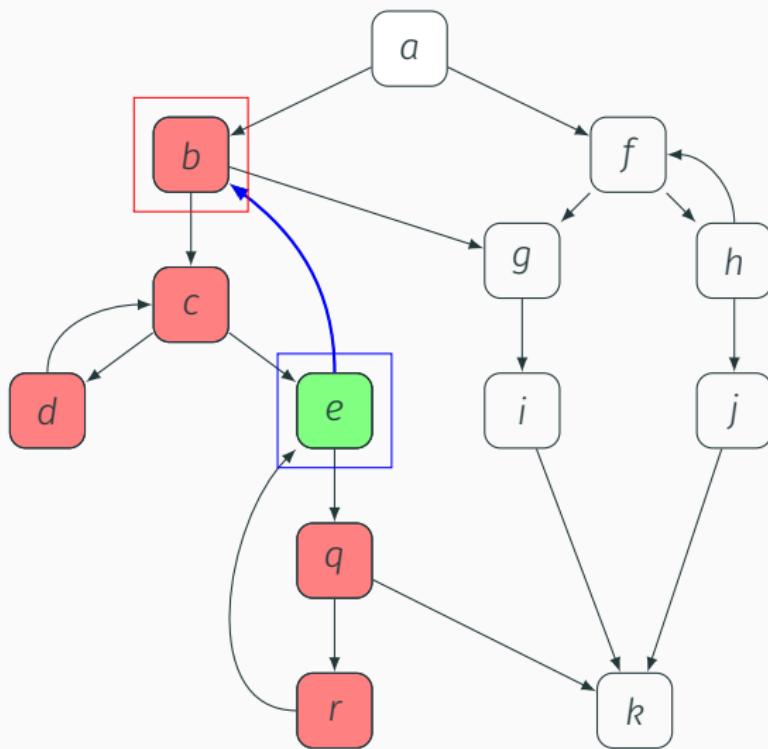
Loops & Loop Nesting Forest

(3) Identify Dominated Blocks



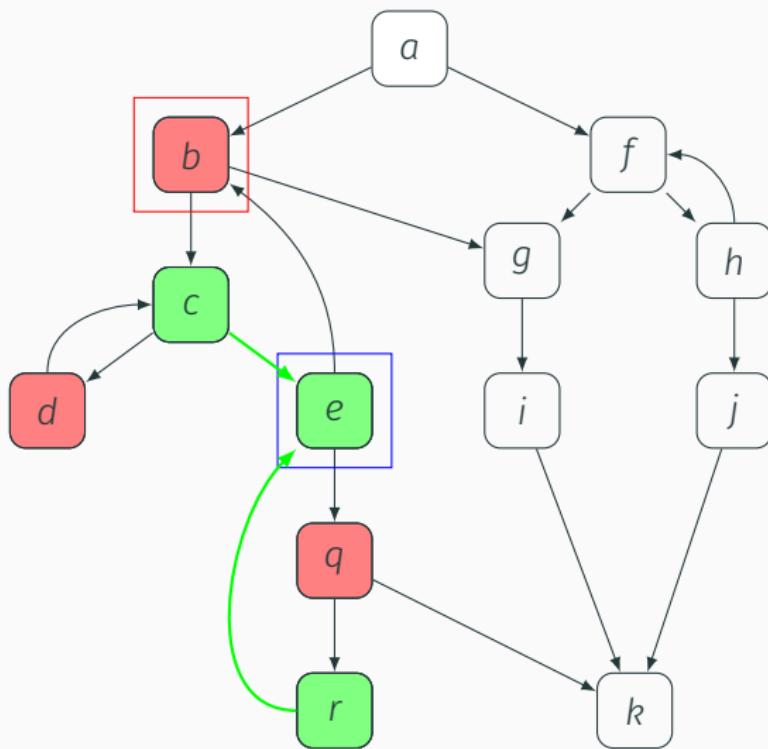
Loops & Loop Nesting Forest

(4) Trace from latch



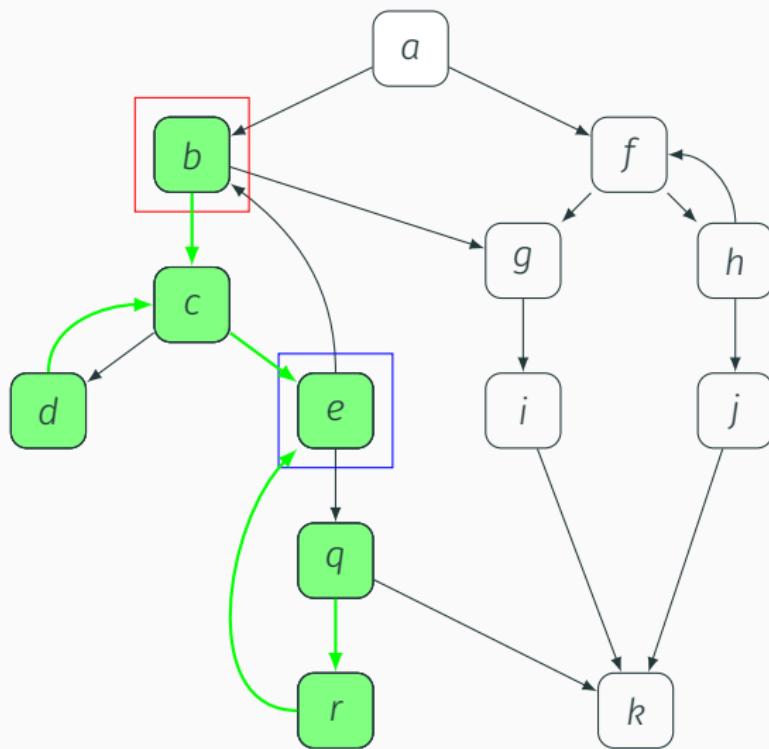
Loops & Loop Nesting Forest

(4) Trace from latch



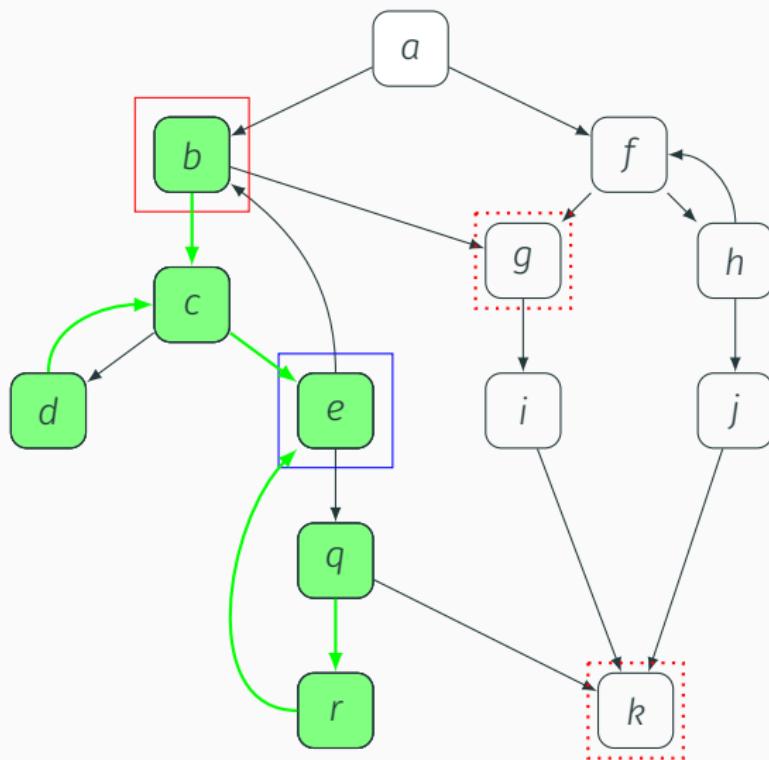
Loops & Loop Nesting Forest

(4) Trace from latch

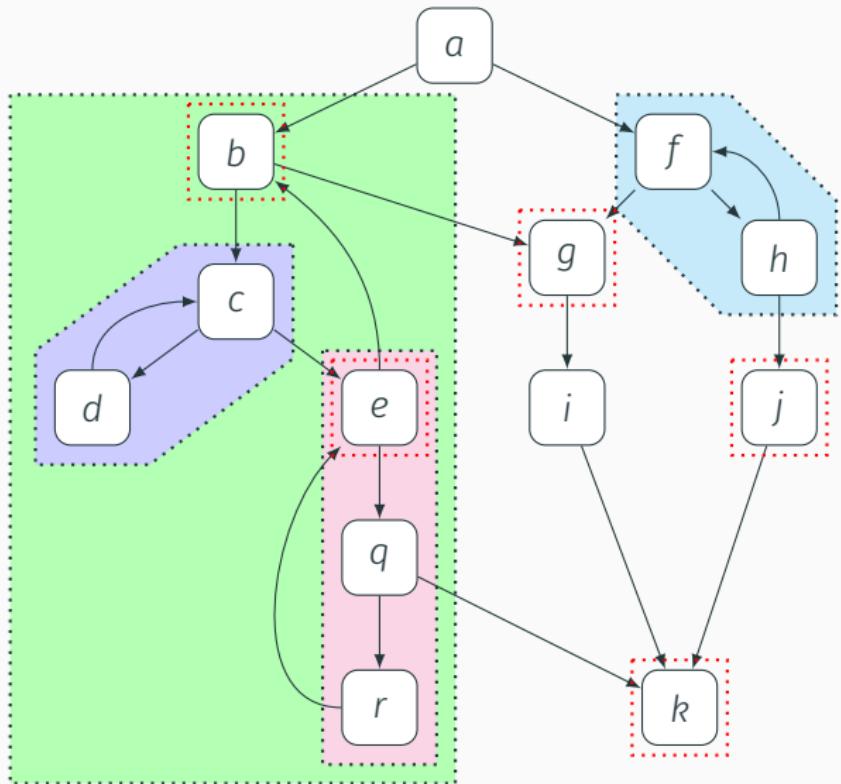


Loops & Loop Nesting Forest

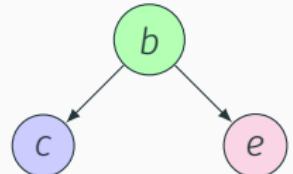
(5) Identify Exits



Loops & Loop Nesting Forest



$\{b, e, c, d, q, r\}$
 $\{g, k\}$



$\{c, d\}$
 $\{e\}$

$\{e, r, q\}$
 $\{b, k\}$

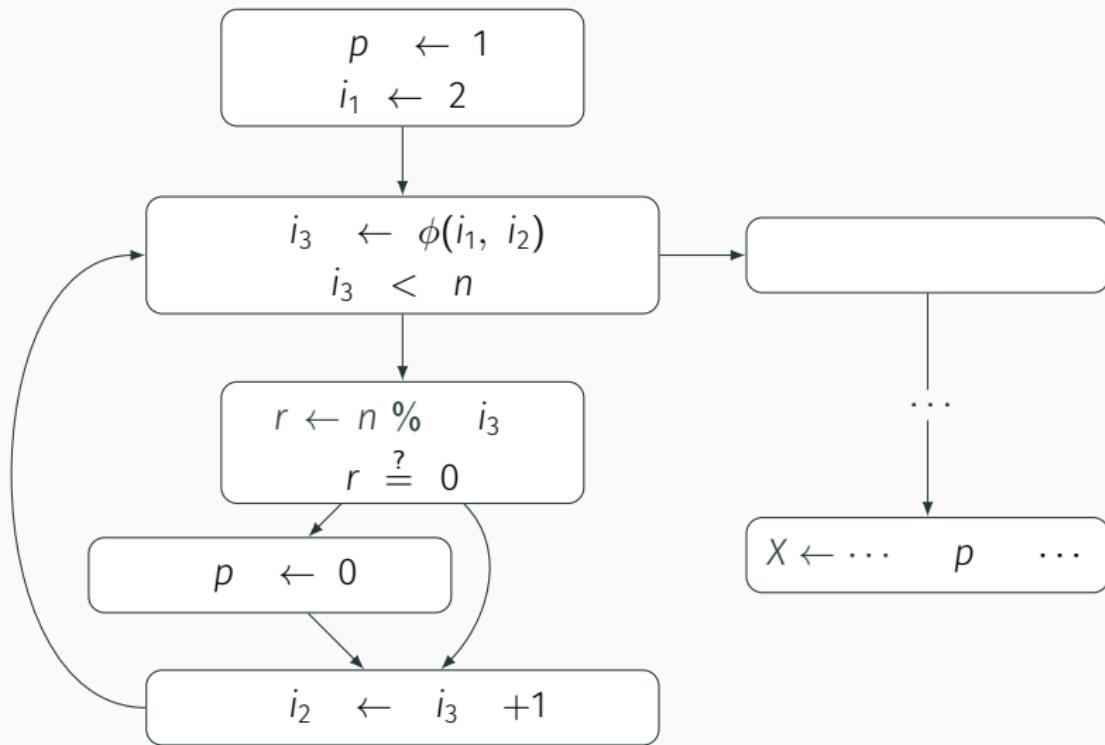


$\{f, h\}$
 $\{g, j\}$

Loop Nesting Forest - An (Extremely) Condensed History

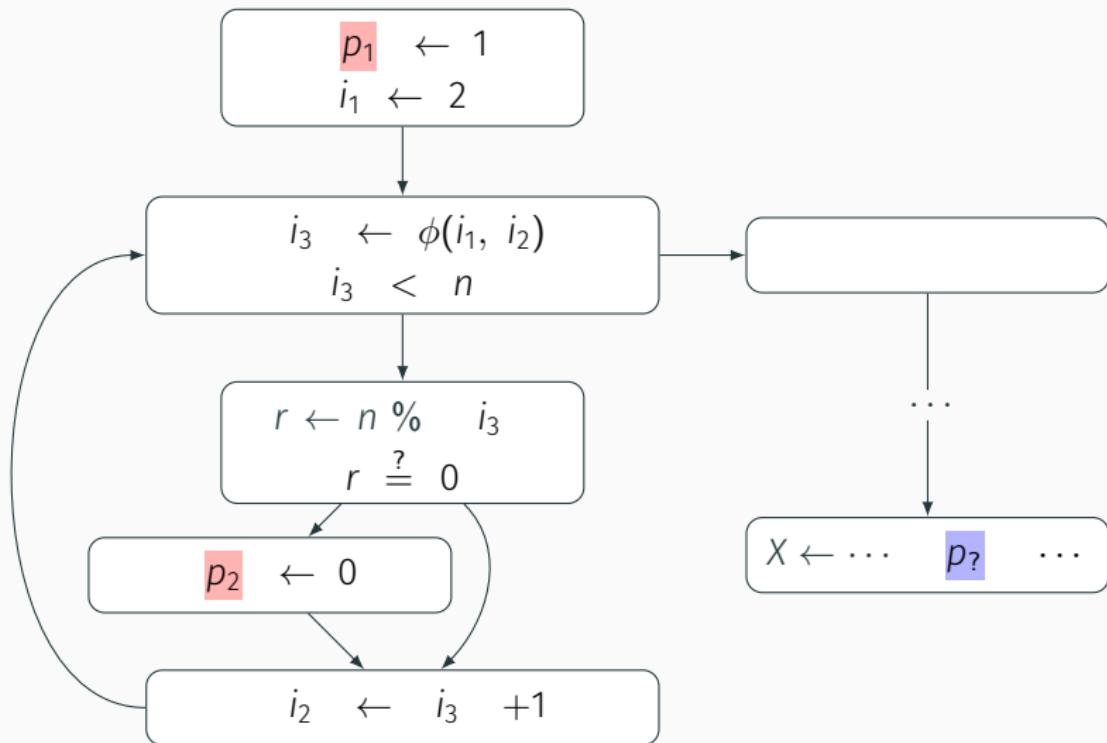
- Tarjan, 1973
- Steensgaard, 1993
- Sreedhar, 1996
- Havlak, 1997

Static Single Assignment Form



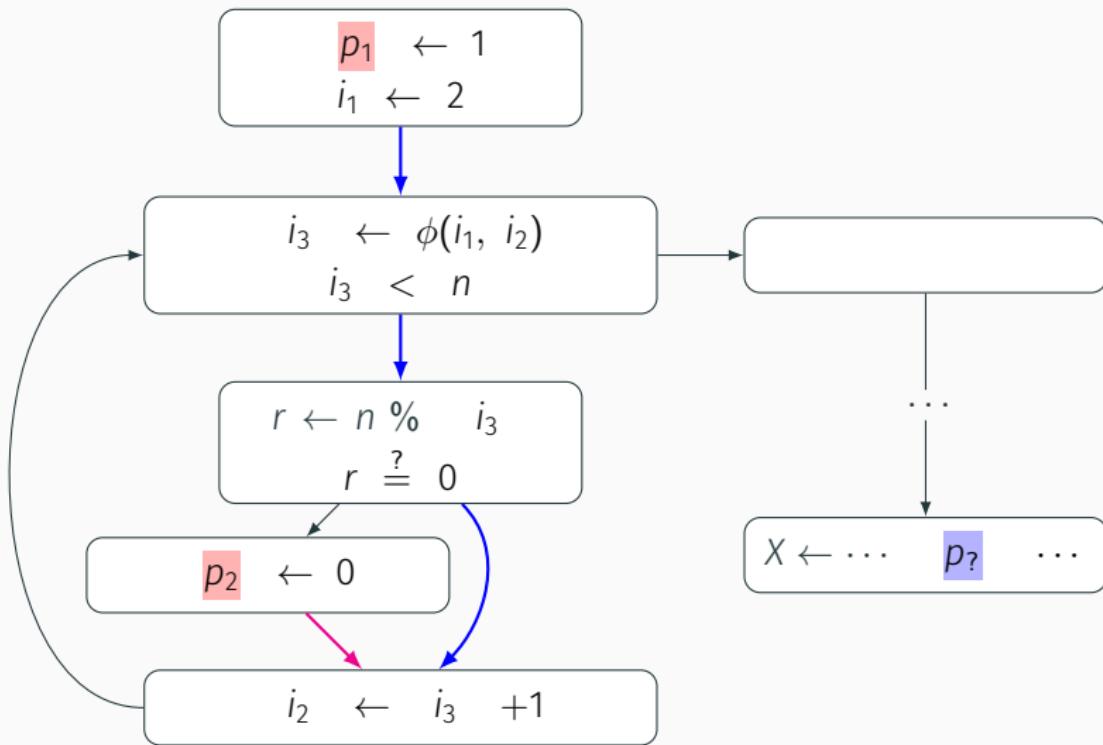
Static Single Assignment Form

(1) Generate unique assignment targets



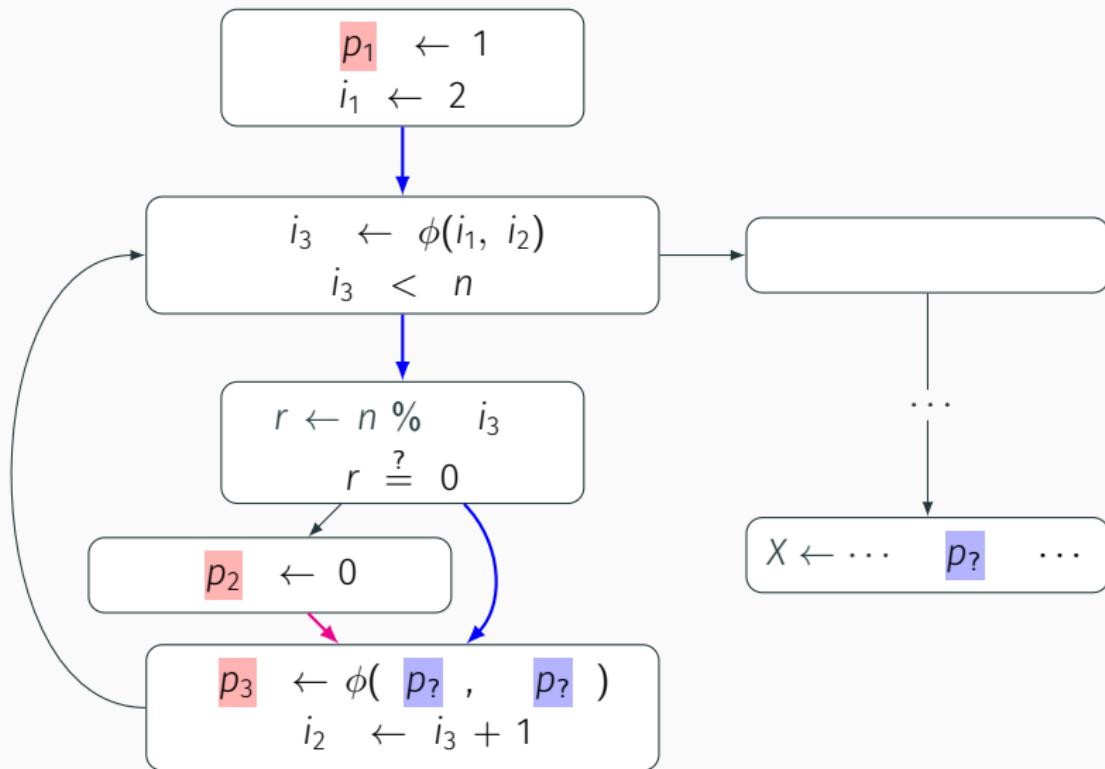
Static Single Assignment Form

(2a) Determine join points with ‘dominance frontier’



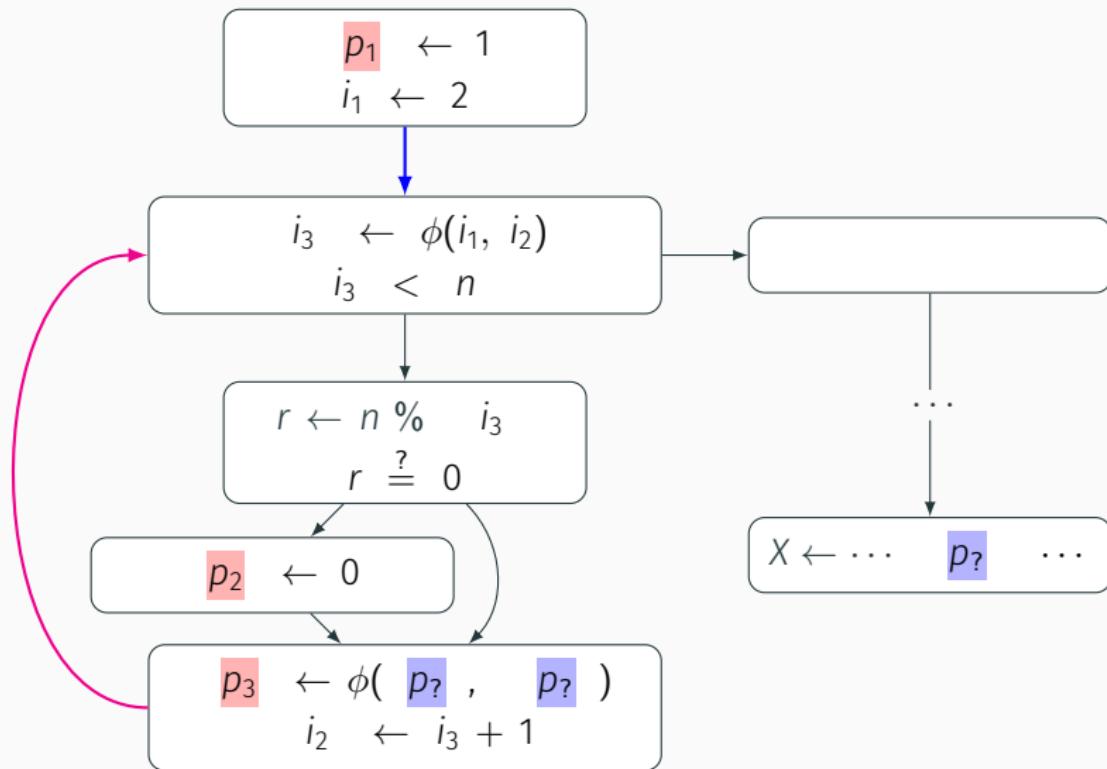
Static Single Assignment Form

(3a) Place ϕ -nodes



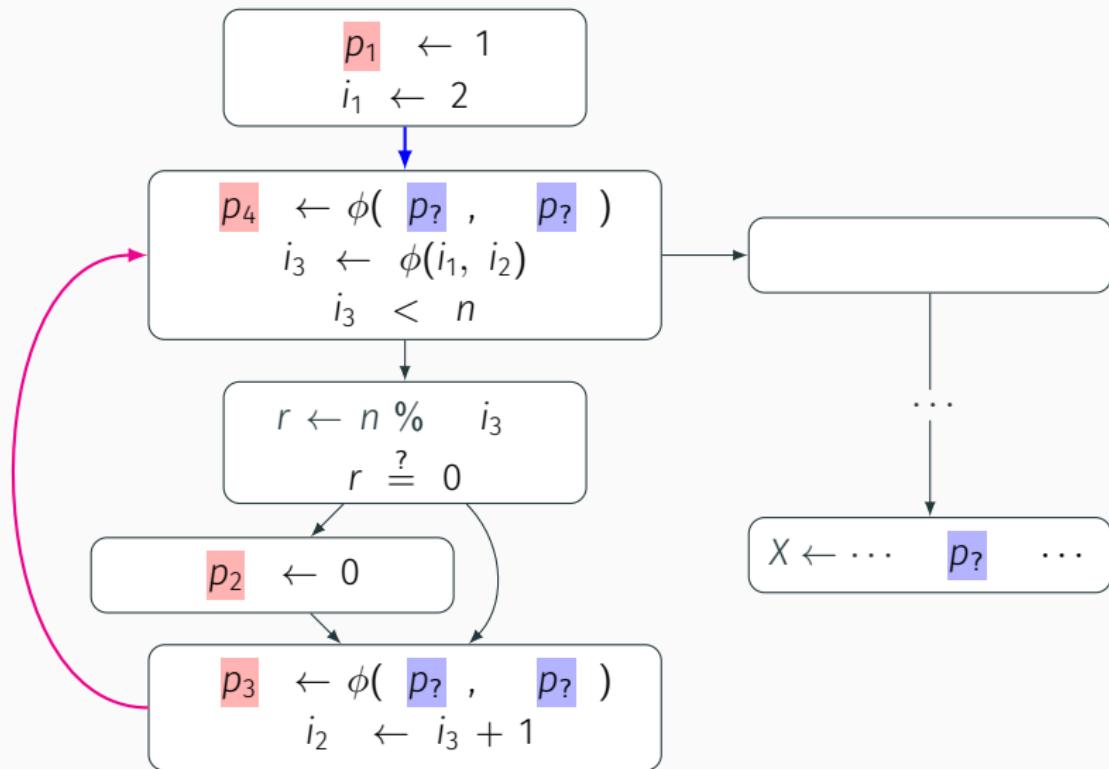
Static Single Assignment Form

(2b) Determine join points with ‘dominance frontier’



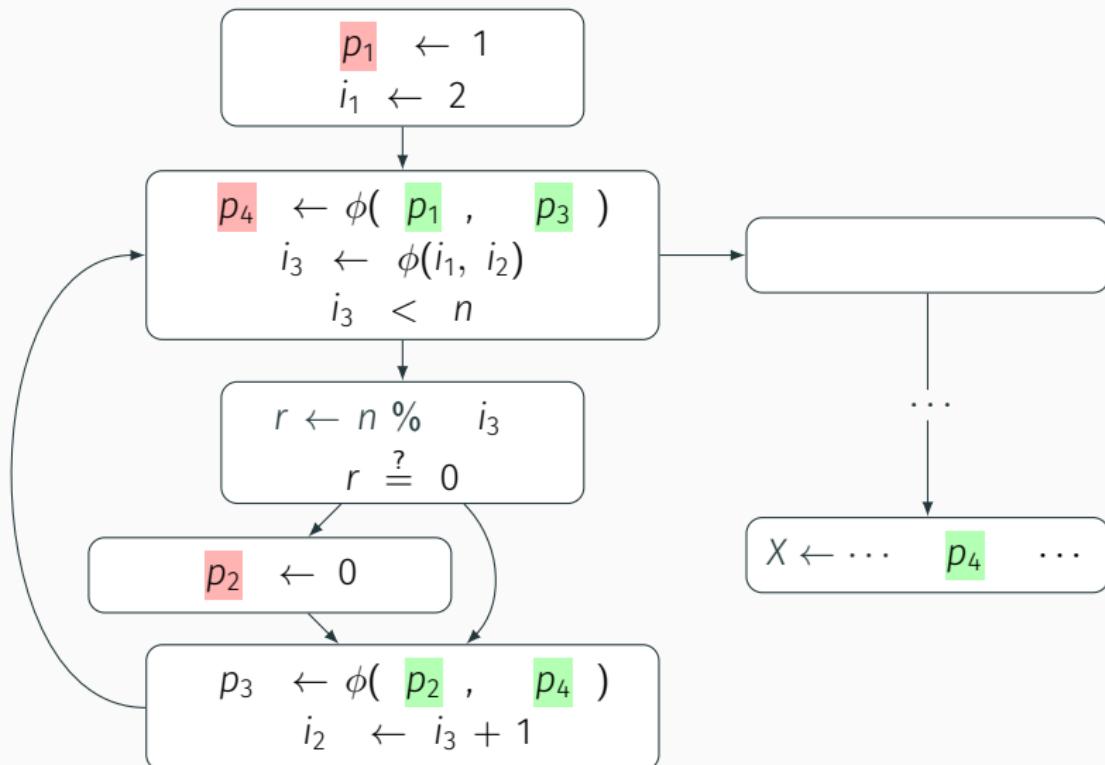
Static Single Assignment Form

(3b) Place ϕ -nodes



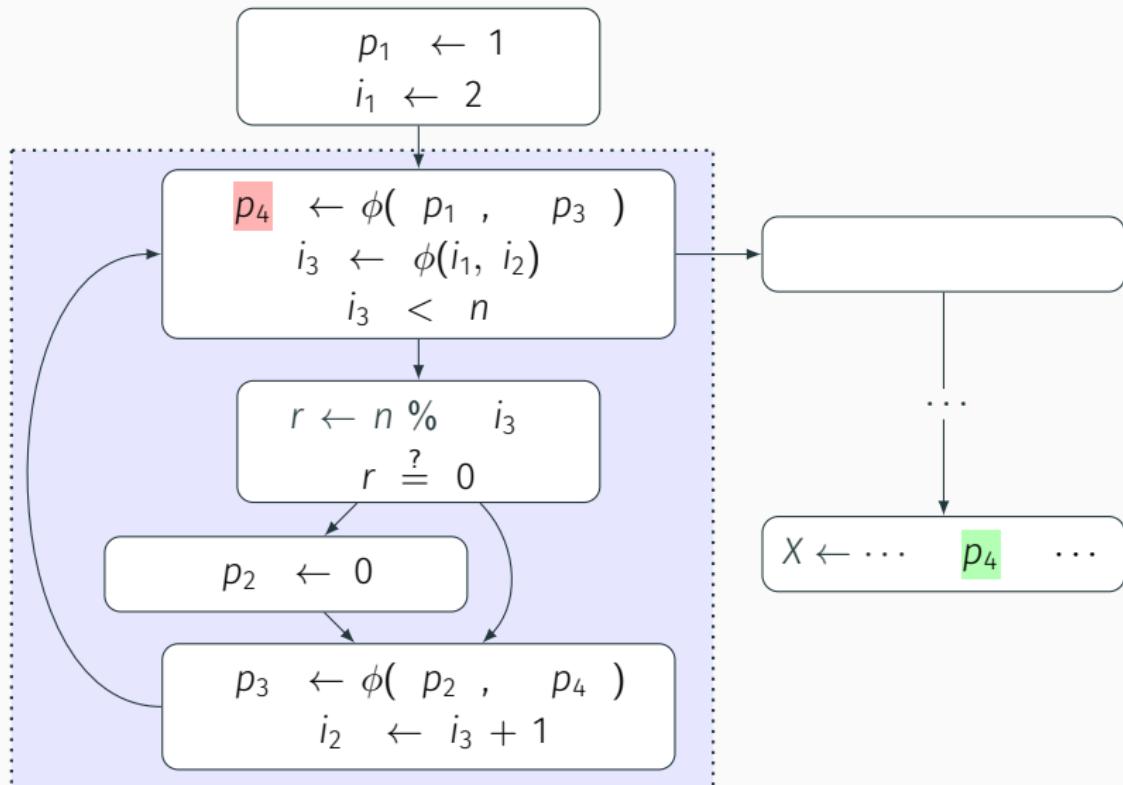
Static Single Assignment Form

(4) Rewrite uses with RD



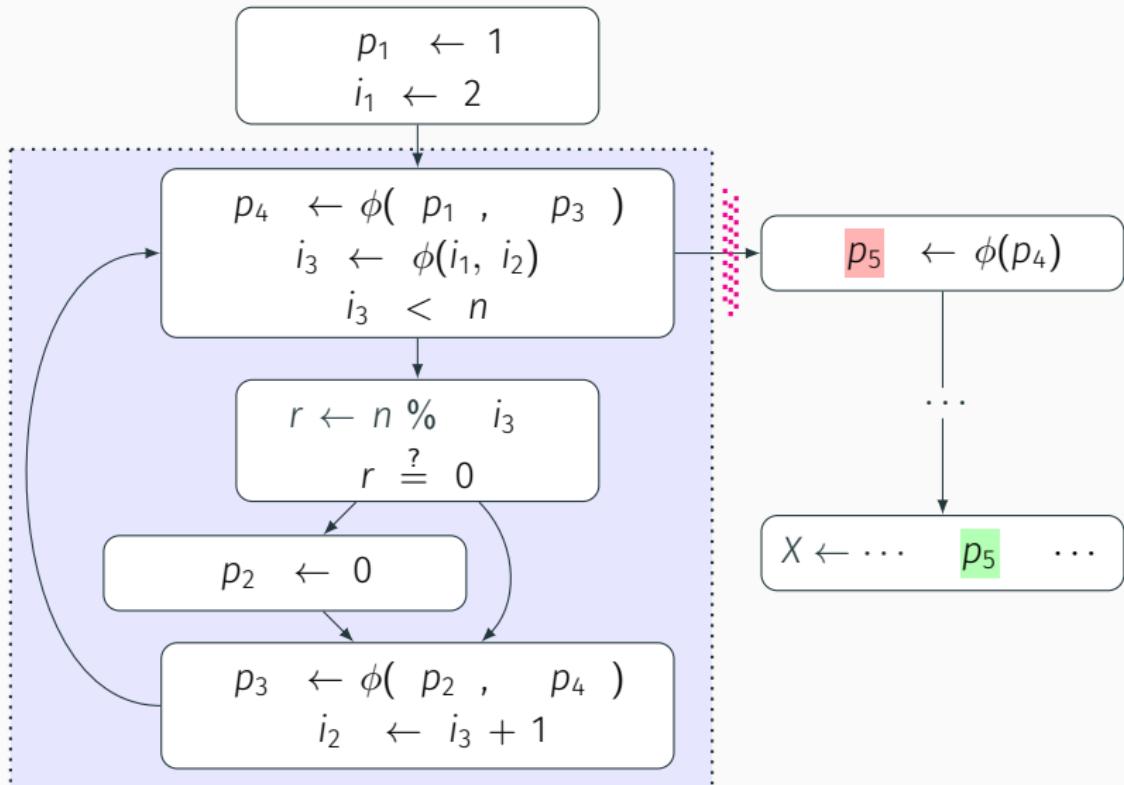
Loop-Closed Static Single Assignment Form

Loop Closed: No uses outside loop of register defined within loop



Loop-Closed Static Single Assignment Form

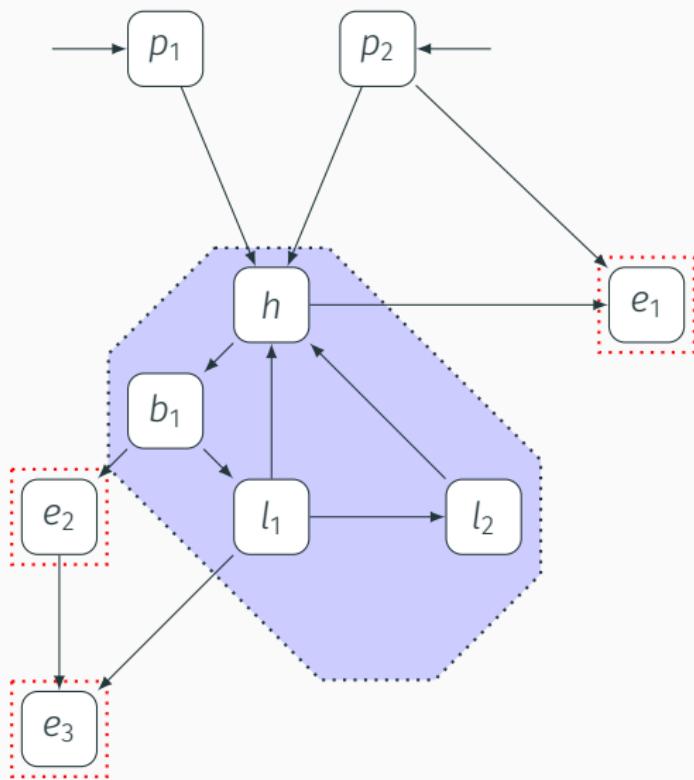
Loop Closed: No uses outside loop of register defined within loop



SSA - An (Extremely) Condensed History

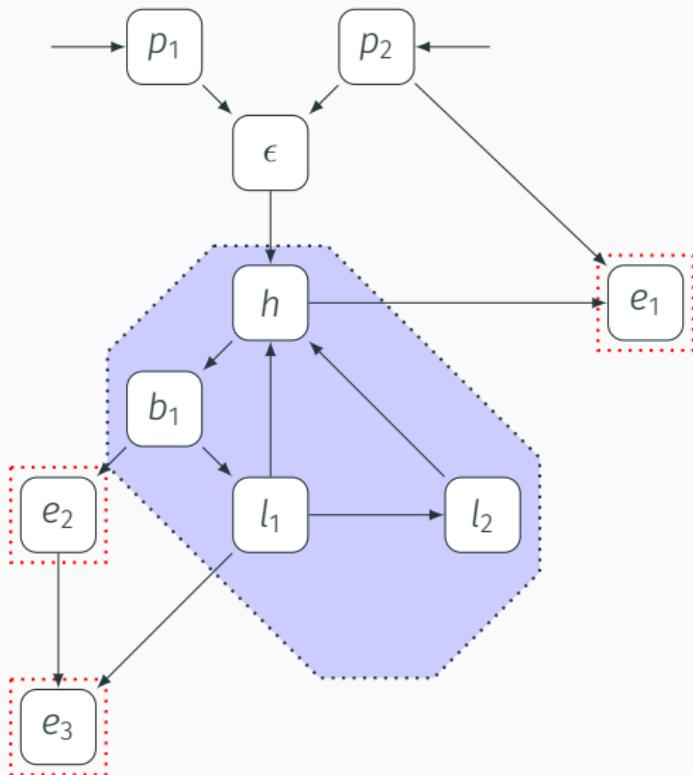
- Cytron & Rosen & Zadeck, 1991
- Choi, 1991
- Briggs, 1998
- Braun & Hack, 2013
- (LCSSA) Zadeck (?), After 1991 (Probably)

Canonical Form



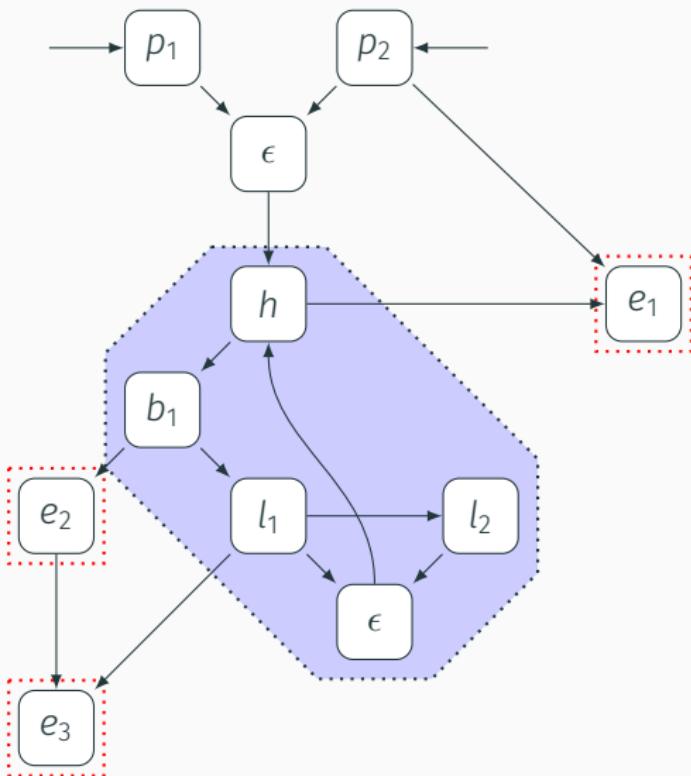
Canonical Form

(Property 1) Dedicated preheader



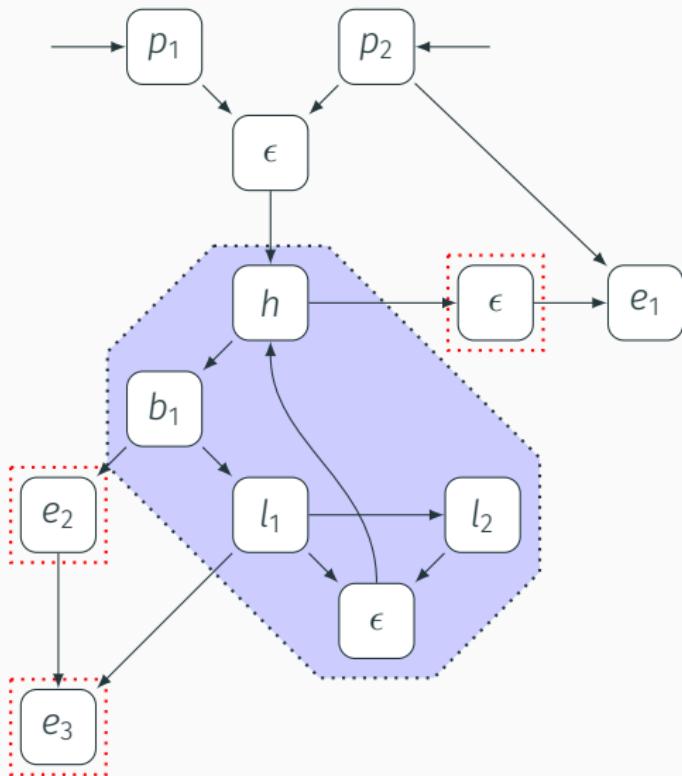
Canonical Form

(Property 2) Single Latch



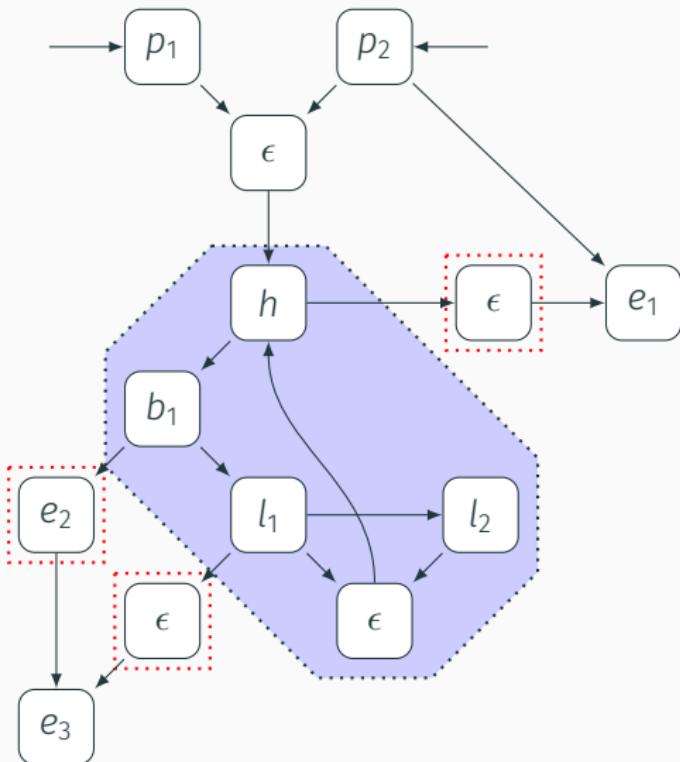
Canonical Form

(Property 3) $\forall b \in \text{exit}(L), \text{pred}(b) \subseteq L$



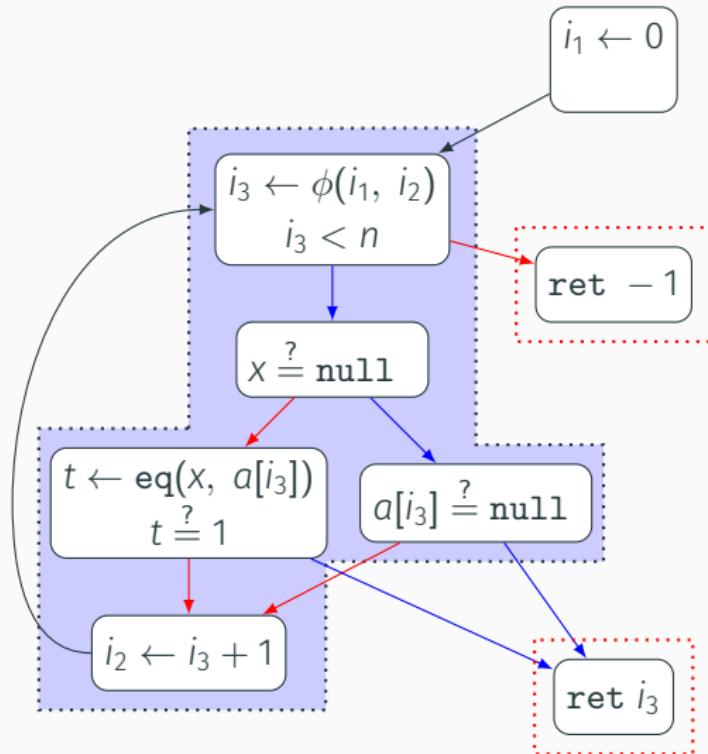
Canonical Form

(Property 3) $\forall b \in \text{exit}(L), \text{pred}(b) \subseteq L$

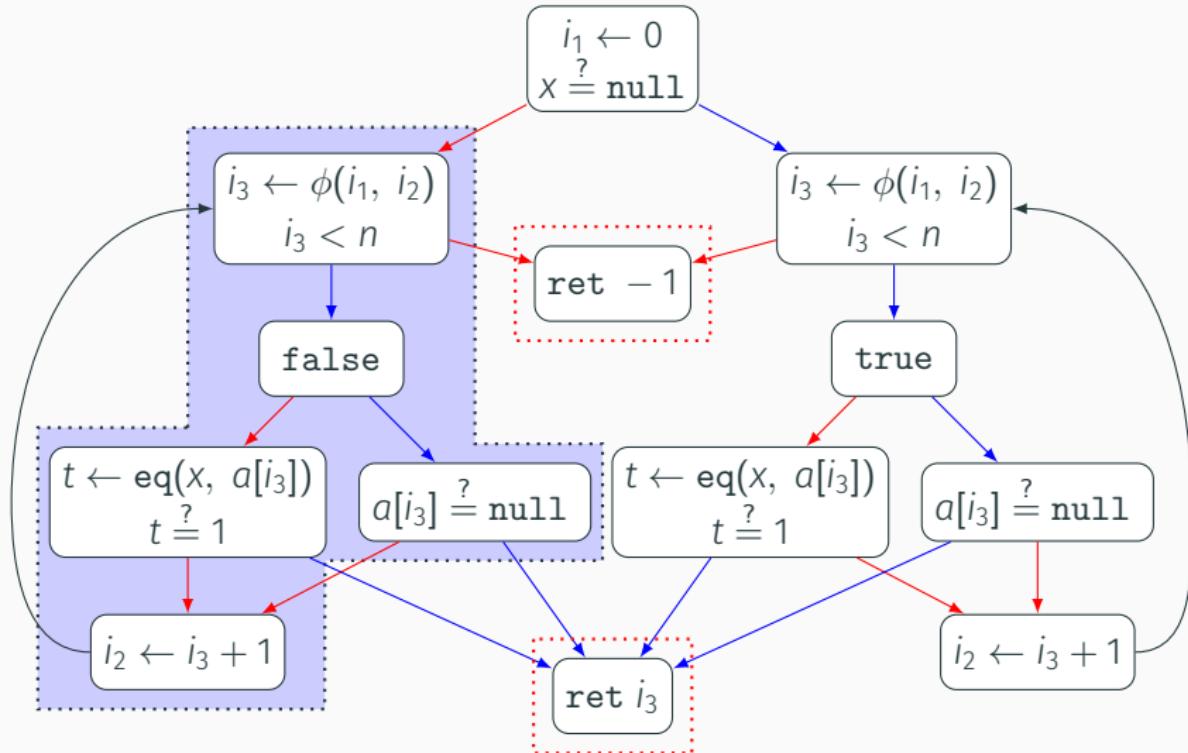


Motivation

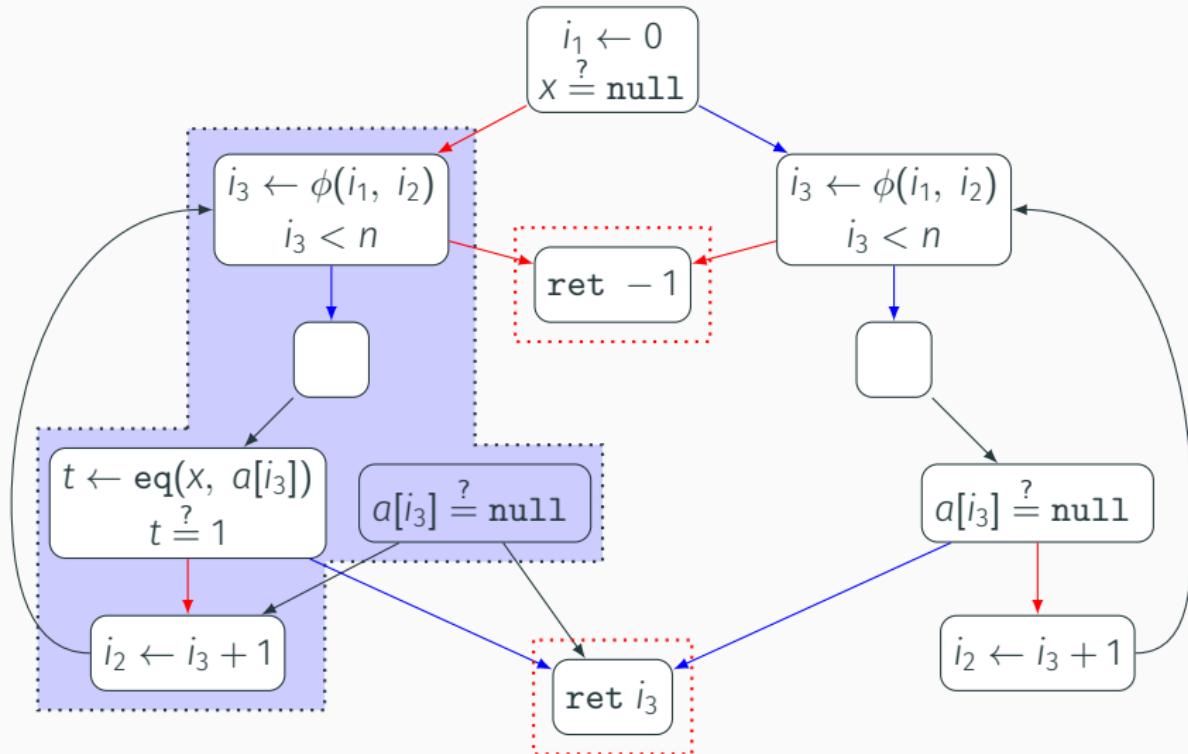
Loop Unswitching + If Simplification



Loop Unswitching + If Simplification



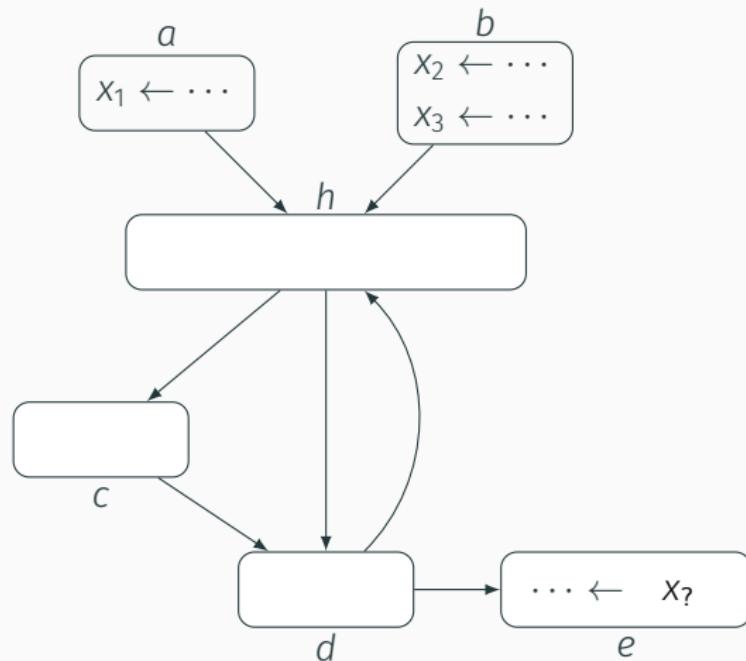
Loop Unswitching + If Simplification



SSA Reconstruction

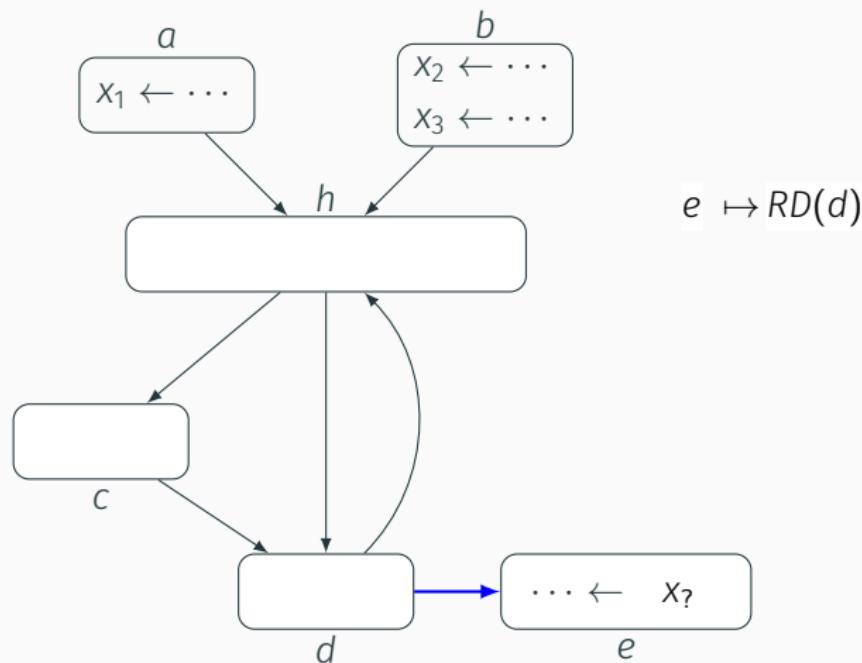
Search-Based Algorithm (Braun 2013)

Starting from a use, search $\overset{\leftarrow}{G}$ for RDs



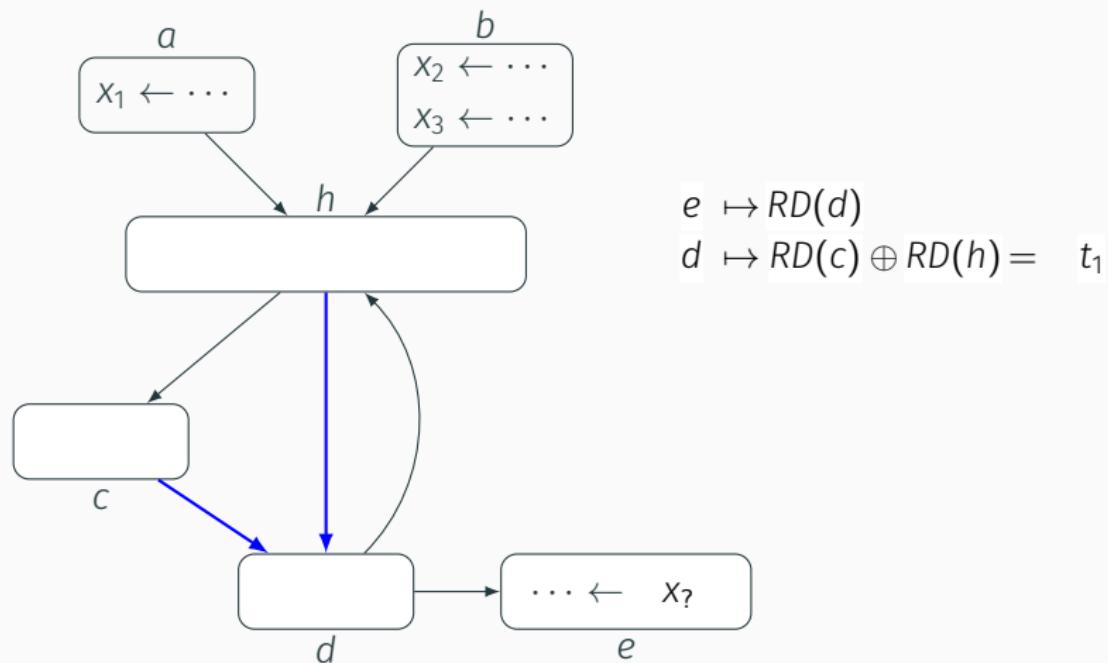
Search-Based Algorithm (Braun 2013)

If a block does not define x , search its predecessors

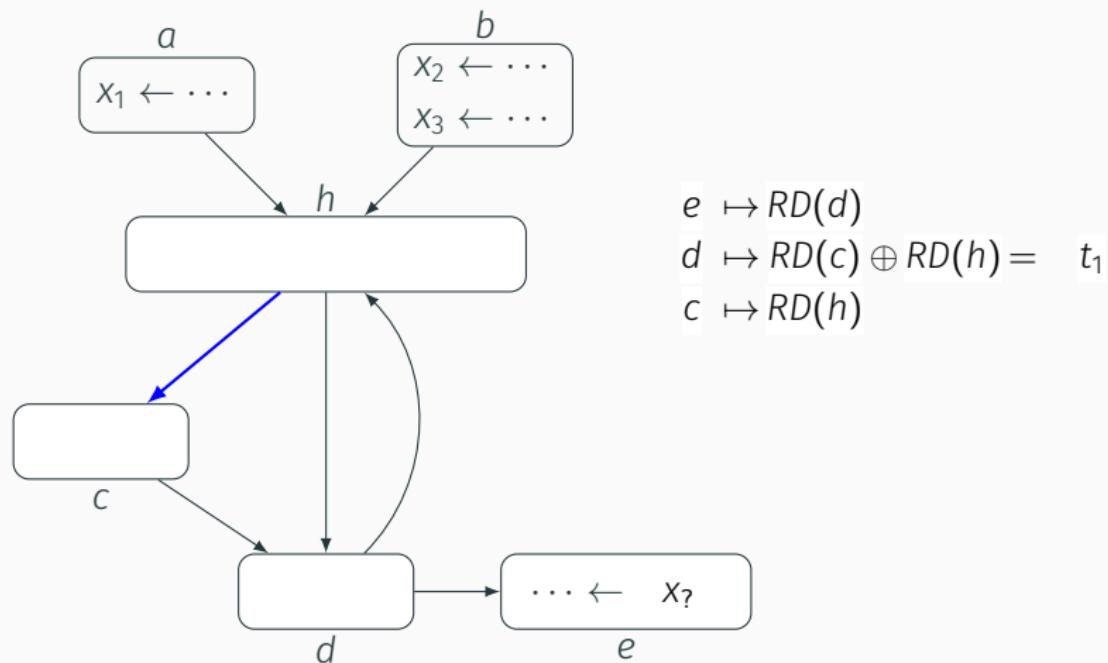


Search-Based Algorithm (Braun 2013)

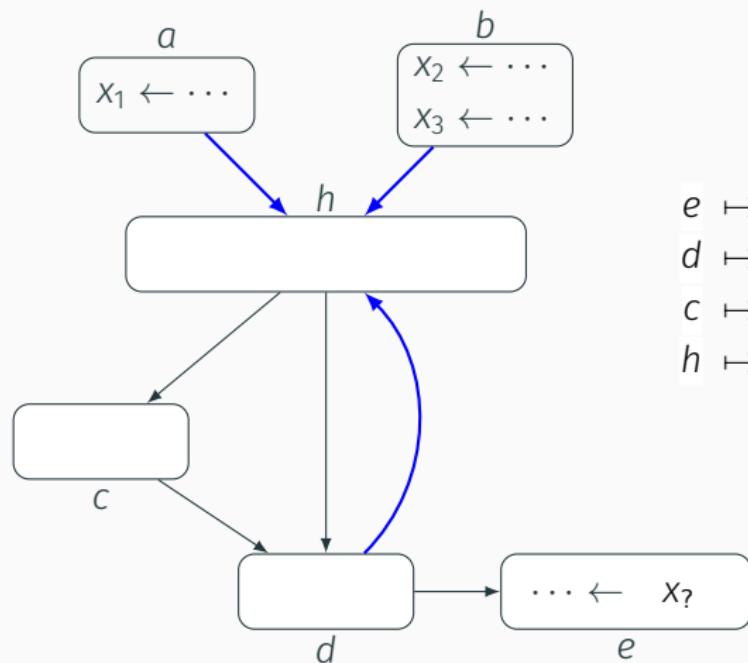
If a block has multiple predecessors, *join* result of predecessors



Search-Based Algorithm (Braun 2013)



Search-Based Algorithm (Braun 2013)



$$e \mapsto RD(d)$$

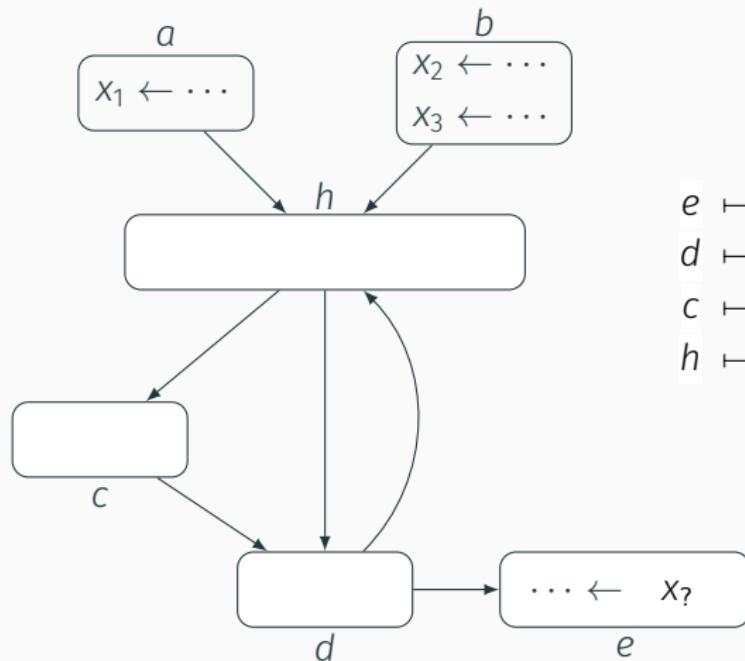
$$d \mapsto RD(c) \oplus RD(h) = t_1$$

$$c \mapsto RD(h)$$

$$h \mapsto RD(a) \oplus RD(b) \oplus RD(d) = t_2$$

Search-Based Algorithm (Braun 2013)

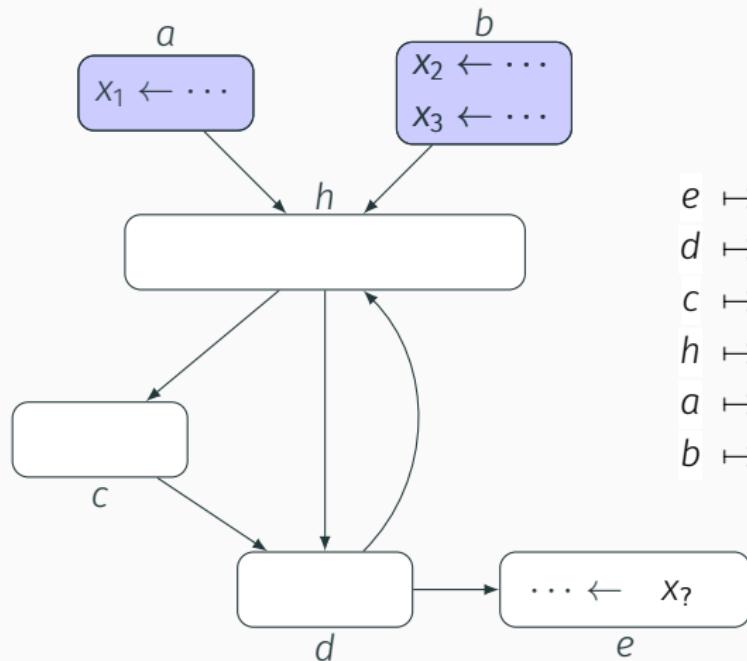
$RD(d)$ term collapses



$$\begin{aligned}e &\mapsto RD(d) \\d &\mapsto RD(c) \oplus RD(h) = t_1 \\c &\mapsto RD(h) \\h &\mapsto RD(a) \oplus RD(b) \oplus t_1 = t_2\end{aligned}$$

Search-Based Algorithm (Braun 2013)

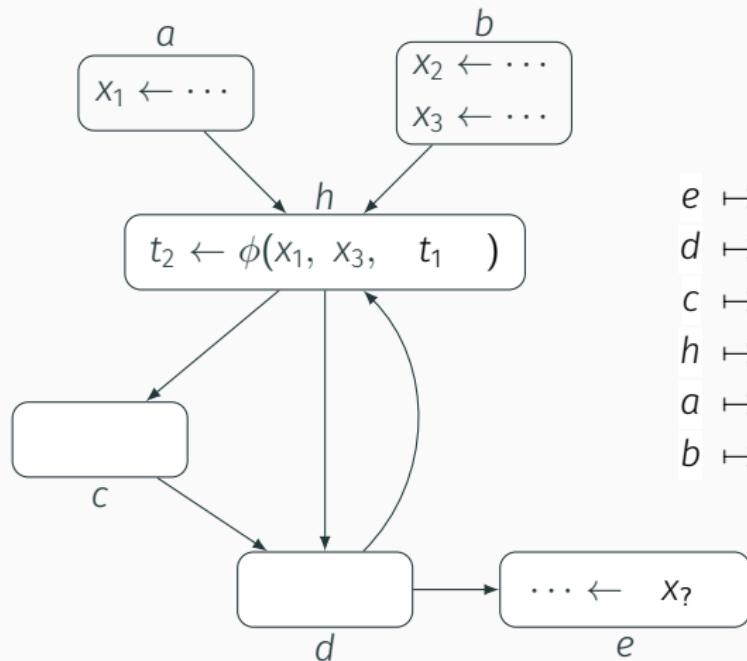
Use **last** definition of x in block



$$\begin{aligned} e &\mapsto RD(d) \\ d &\mapsto RD(c) \oplus RD(h) = t_1 \\ c &\mapsto RD(h) \\ h &\mapsto RD(a) \oplus RD(b) \oplus t_1 = t_2 \\ a &\mapsto x_1 \\ b &\mapsto x_3 \end{aligned}$$

Search-Based Algorithm (Braun 2013)

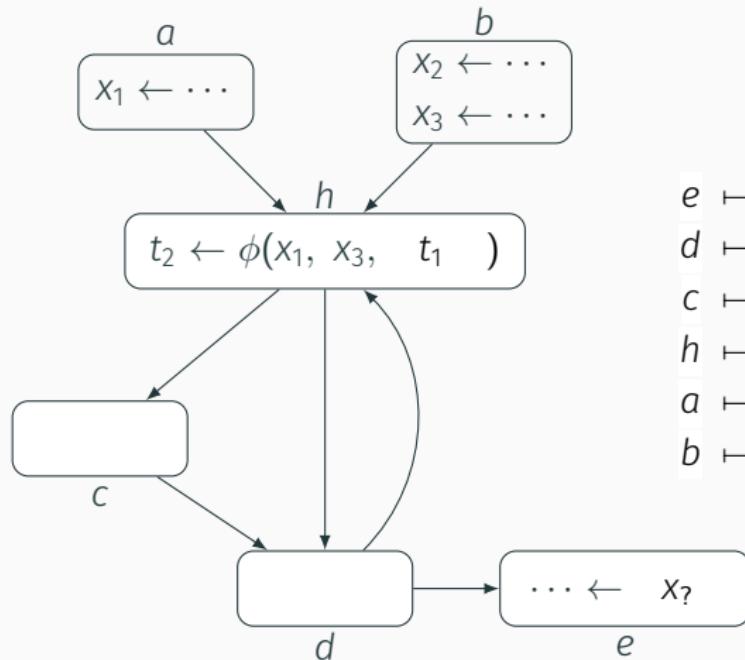
$RD(a)$ and $RD(b)$ terms collapse, $RD(h)$ has concrete ϕ -arguments



$$\begin{aligned} e &\mapsto RD(d) \\ d &\mapsto RD(c) \oplus RD(h) = t_1 \\ c &\mapsto RD(h) \\ h &\mapsto x_1 \oplus x_3 \oplus t_1 = t_2 \\ a &\mapsto x_1 \\ b &\mapsto x_3 \end{aligned}$$

Search-Based Algorithm (Braun 2013)

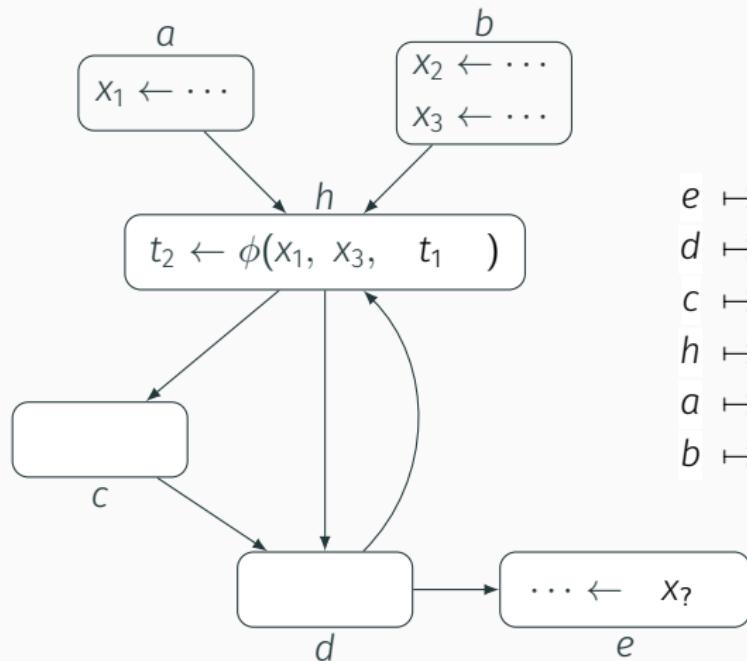
$RD(h)$ term collapses



$$\begin{aligned} e &\mapsto RD(d) \\ d &\mapsto RD(c) \oplus t_2 = t_1 \\ c &\mapsto t_2 \\ h &\mapsto x_1 \oplus x_3 \oplus t_1 = t_2 \\ a &\mapsto x_1 \\ b &\mapsto x_3 \end{aligned}$$

Search-Based Algorithm (Braun 2013)

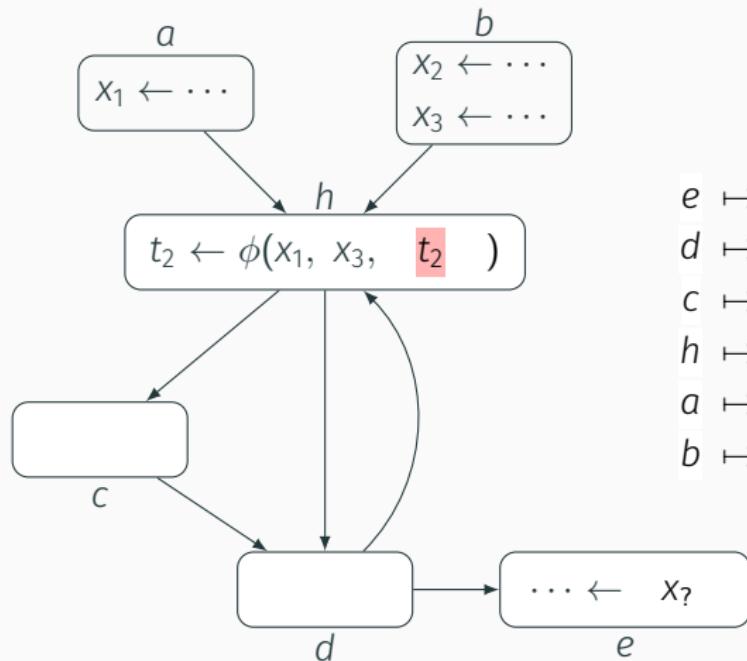
$RD(c)$ term collapses



$$\begin{aligned}e &\mapsto RD(d) \\d &\mapsto t_2 \oplus t_2 = t_1 \\c &\mapsto t_2 \\h &\mapsto x_1 \oplus x_3 \oplus t_1 = t_2 \\a &\mapsto x_1 \\b &\mapsto x_3\end{aligned}$$

Search-Based Algorithm (Braun 2013)

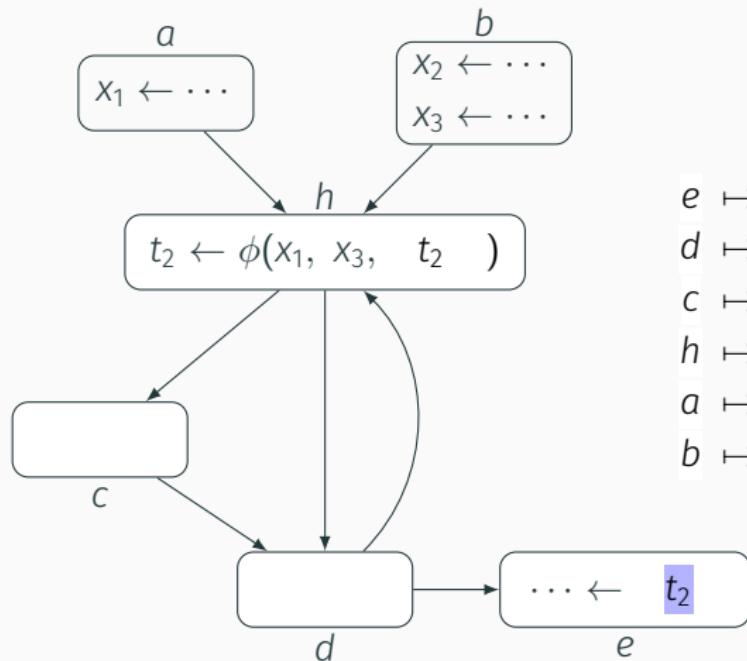
$t_1 = \phi(t_2, t_2)$ is trivially unnecessary



$$\begin{aligned} e &\mapsto RD(d) \\ d &\mapsto t_2 \oplus t_2 = t_2 \\ c &\mapsto t_2 \\ h &\mapsto x_1 \oplus x_3 \oplus t_2 = t_2 \\ a &\mapsto x_1 \\ b &\mapsto x_3 \end{aligned}$$

Search-Based Algorithm (Braun 2013)

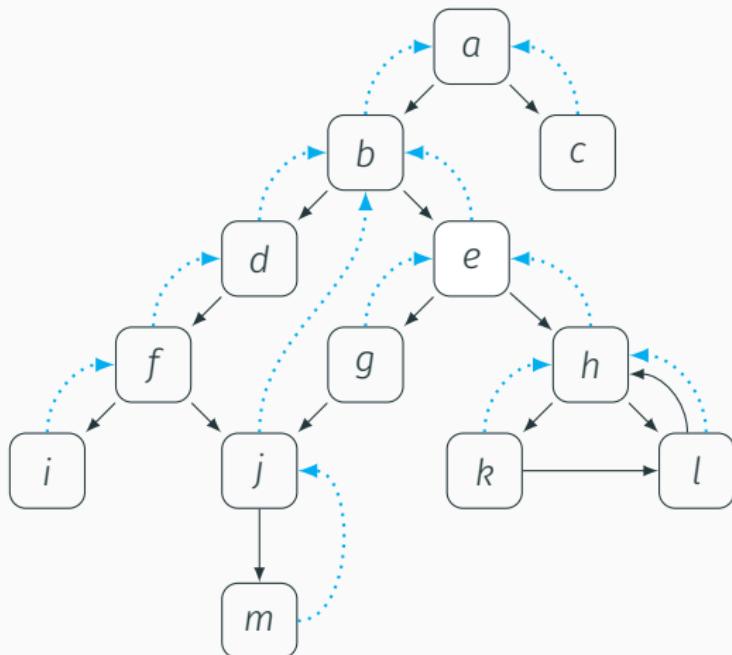
$RD(d)$ term collapses, $RD(e)$ has a solution



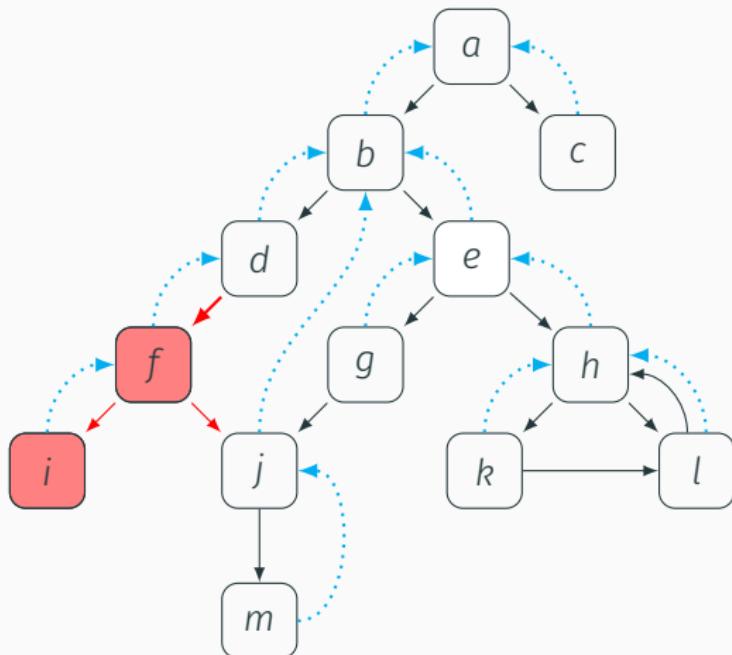
$$\begin{aligned} e &\mapsto t_2 \\ d &\mapsto t_2 \oplus t_2 = t_2 \\ c &\mapsto t_2 \\ h &\mapsto x_1 \oplus x_3 \oplus t_2 = t_2 \\ a &\mapsto x_1 \\ b &\mapsto x_3 \end{aligned}$$

Dominator Tree Reconstruction

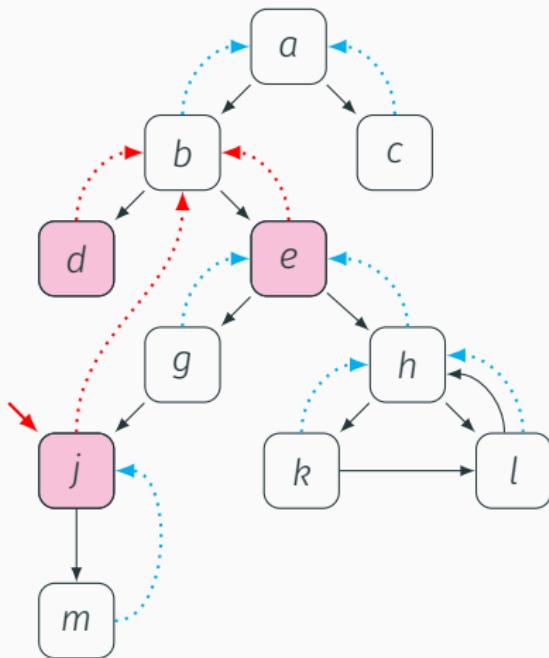
Edge Deletion (Ramalingam & Reps 1994)



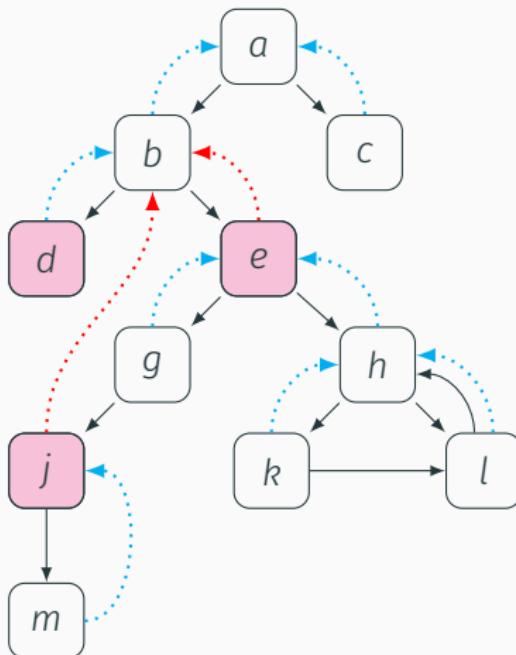
Edge Deletion (Ramalingam & Reps 1994)



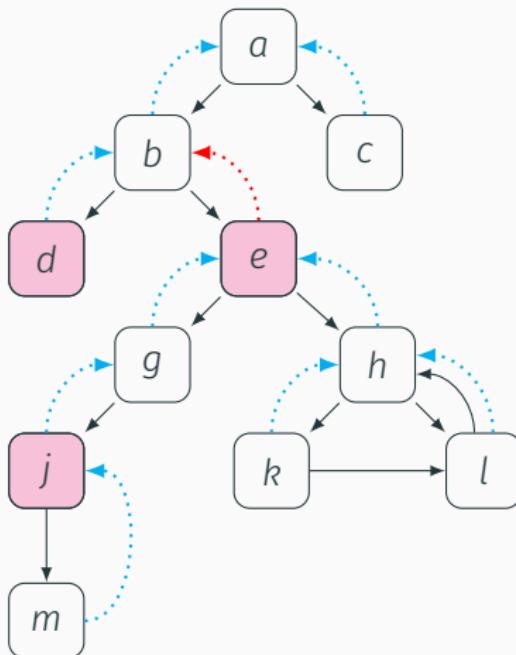
Edge Deletion (Ramalingam & Reps 1994)



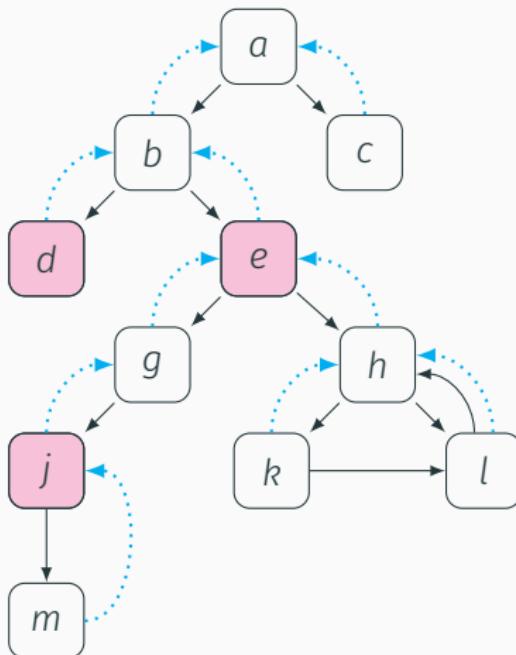
Edge Deletion (Ramalingam & Reps 1994)



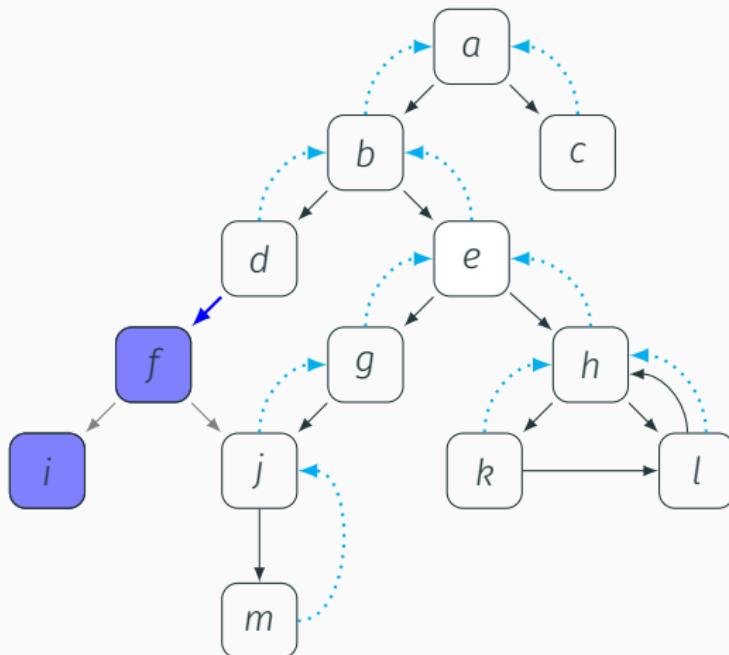
Edge Deletion (Ramalingam & Reps 1994)



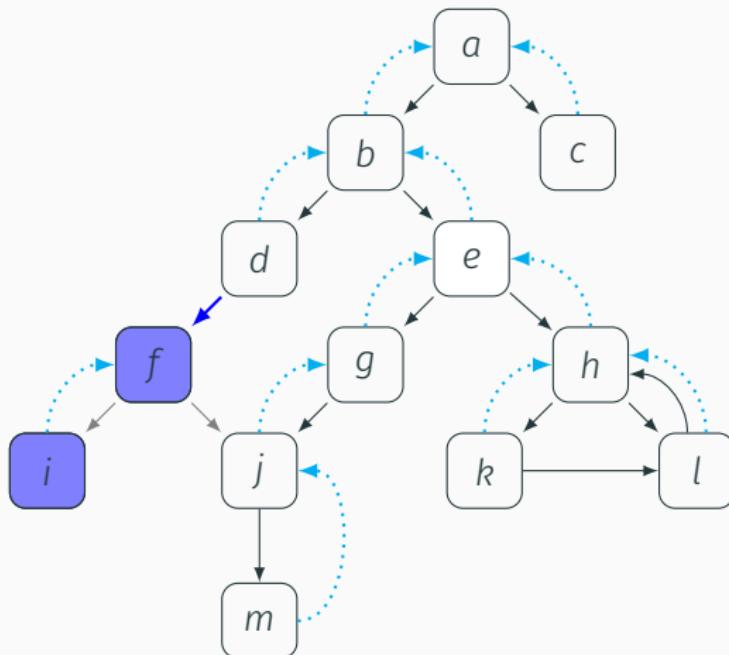
Edge Deletion (Ramalingam & Reps 1994)



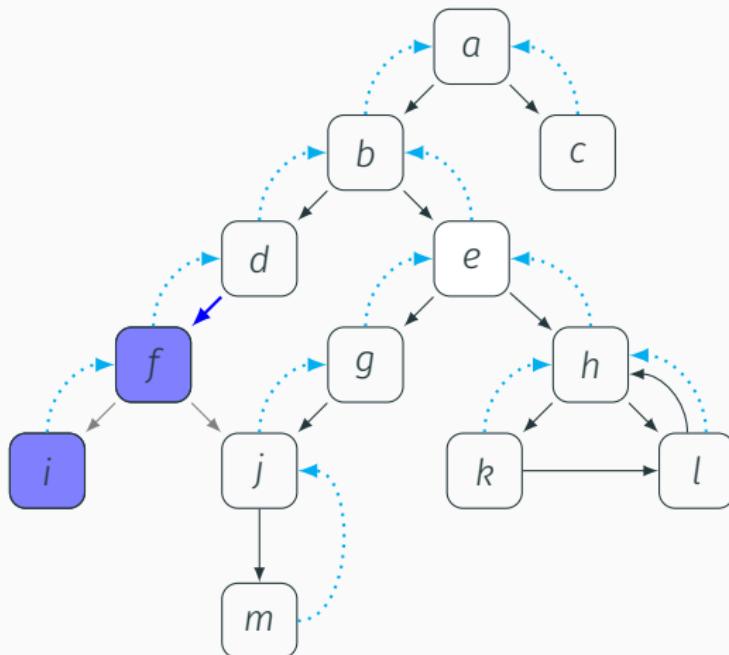
Edge Insertion (Ramalingam & Reps 1994)



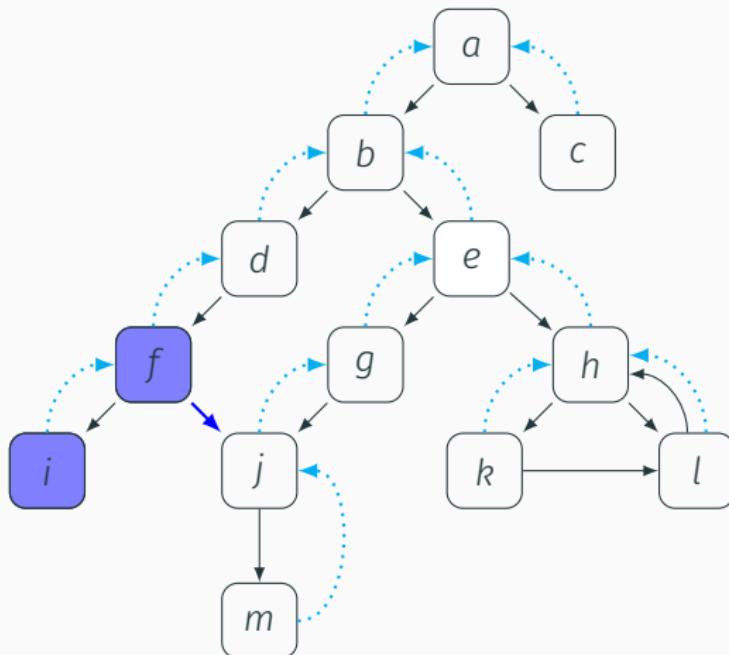
Edge Insertion (Ramalingam & Reps 1994)



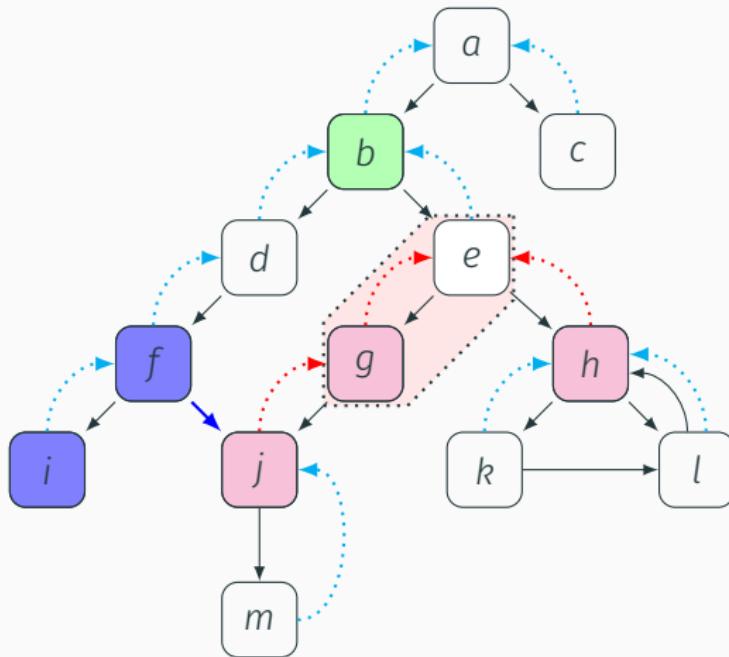
Edge Insertion (Ramalingam & Reps 1994)



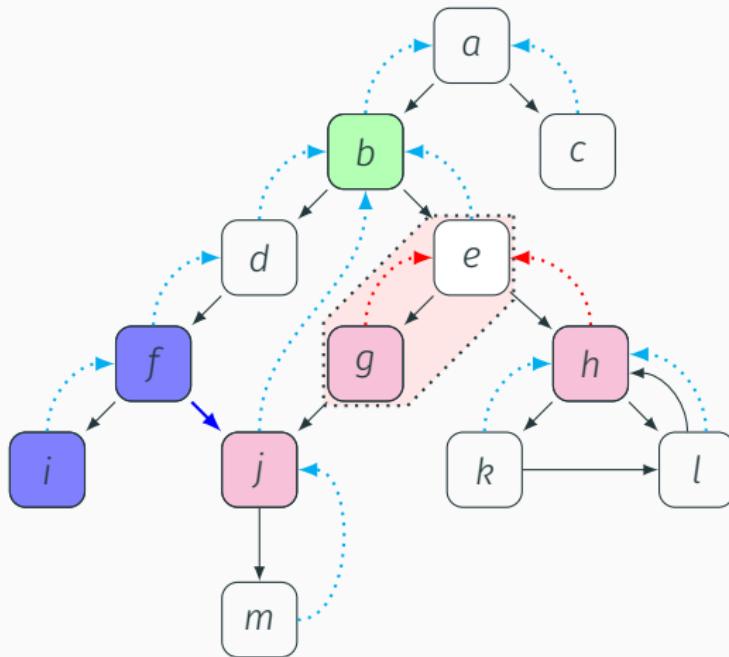
Edge Insertion (Ramalingam & Reps 1994)



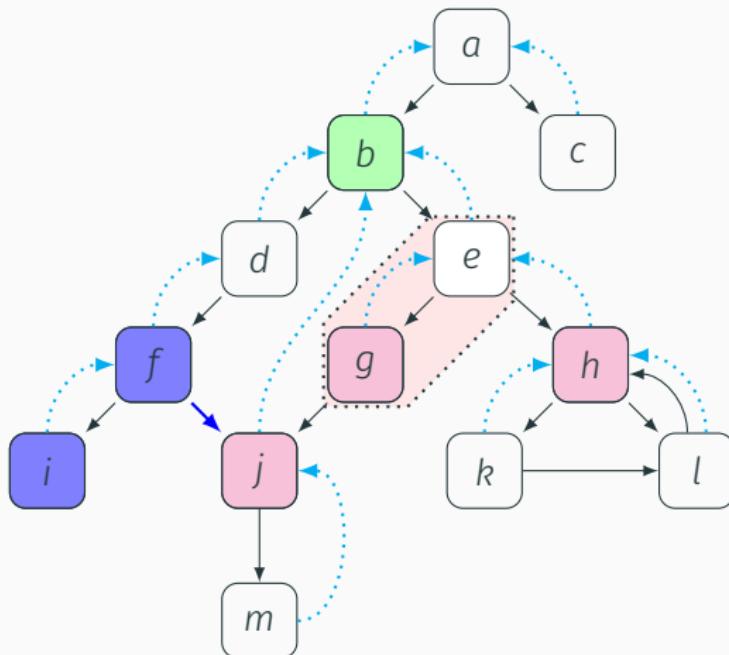
Edge Insertion (Ramalingam & Reps 1994)



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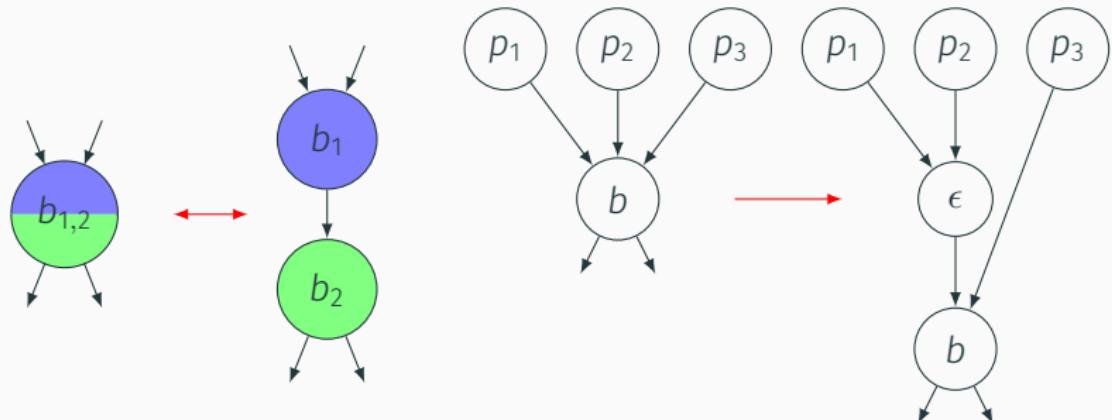


Edge Insertion (Ramalingam & Reps 1994)

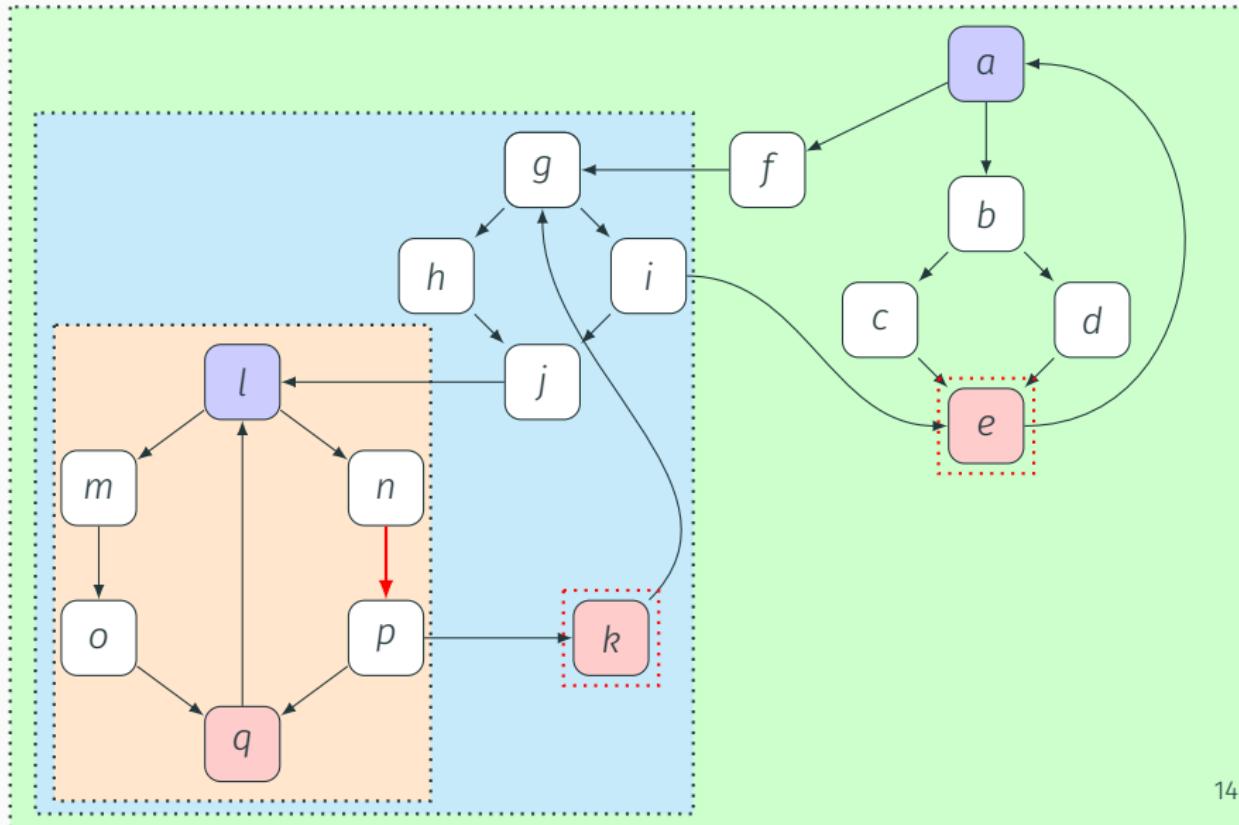


Canonical Form Preservation

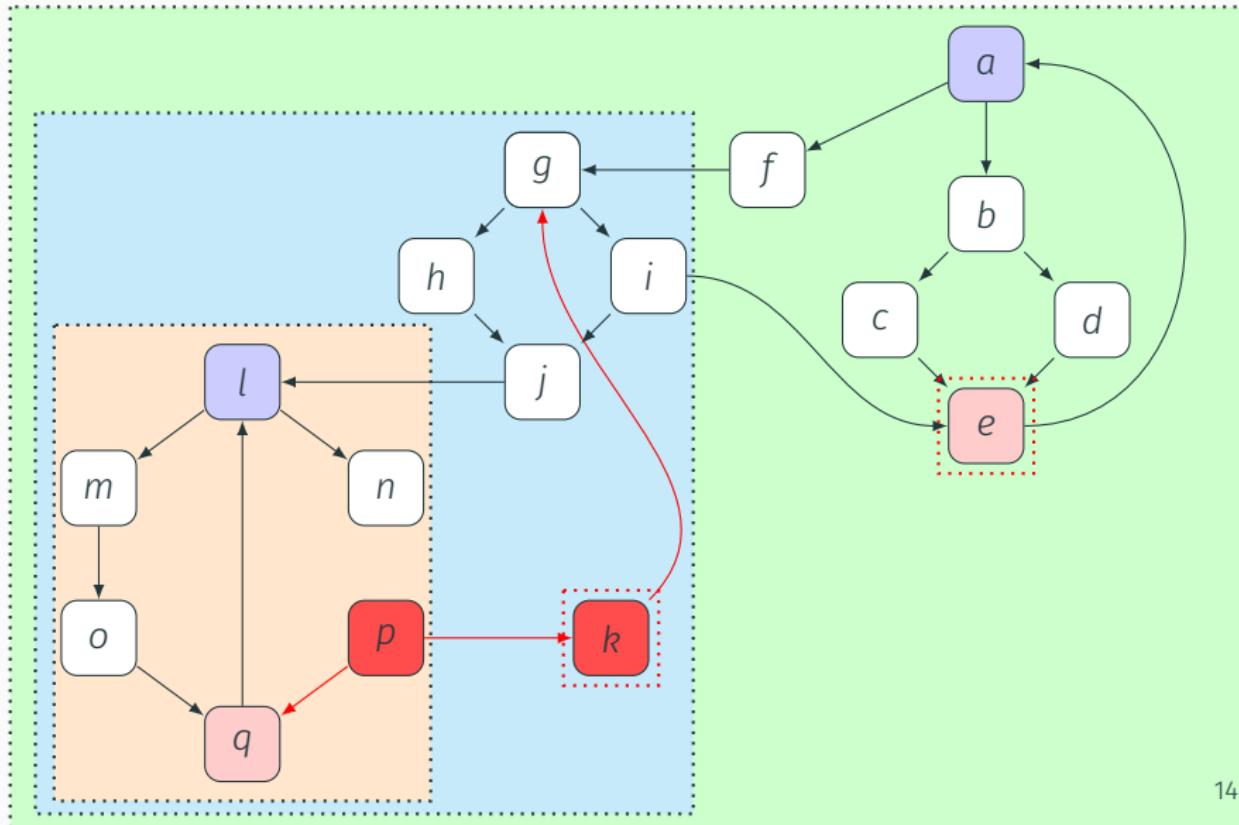
Block Splitting / Collapsing & Edge-Set Splitting



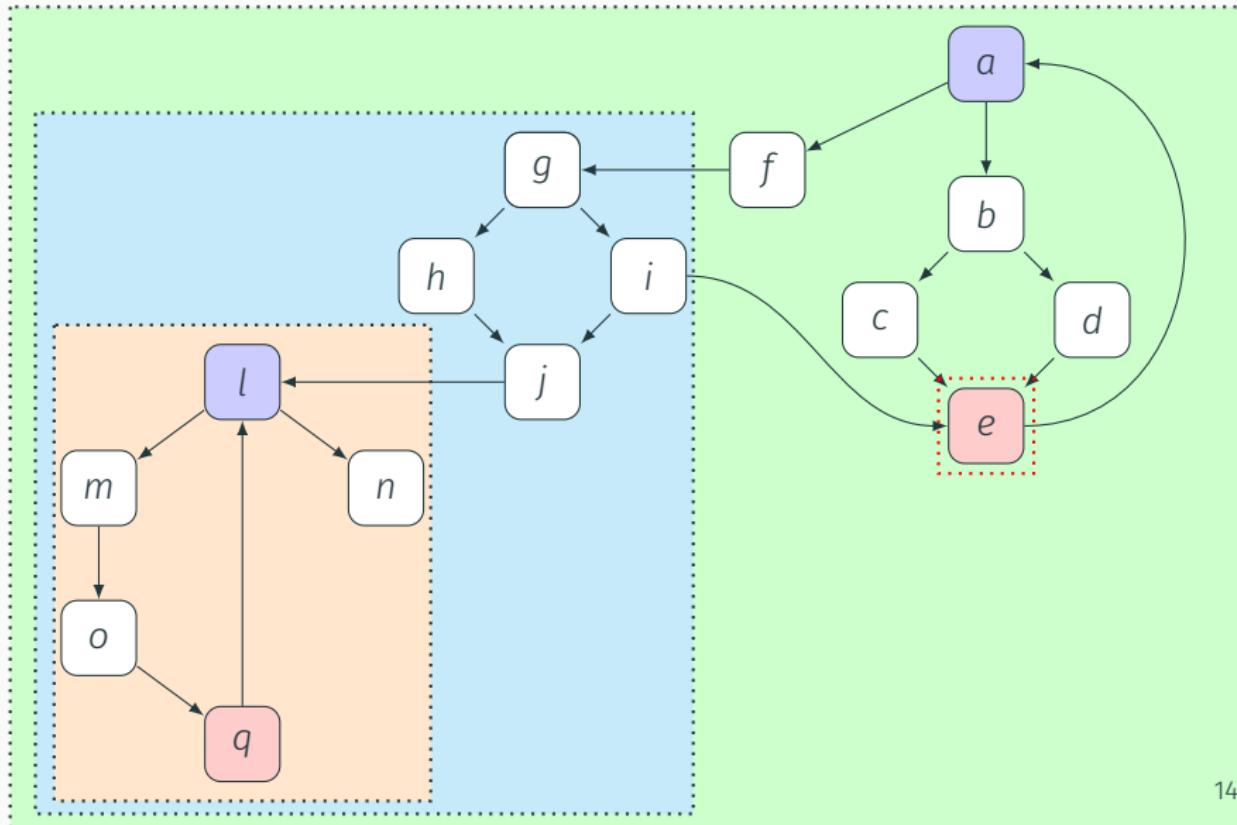
Edge Deletion



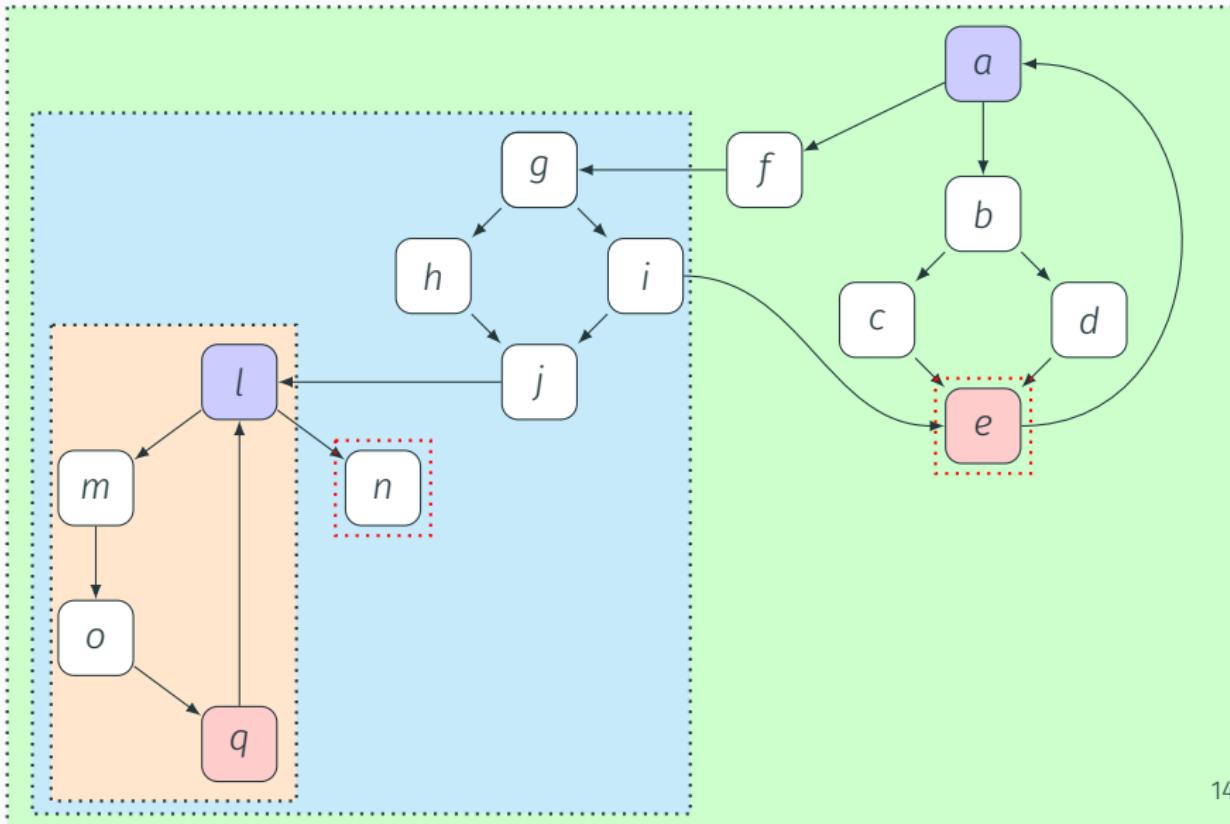
Edge Deletion



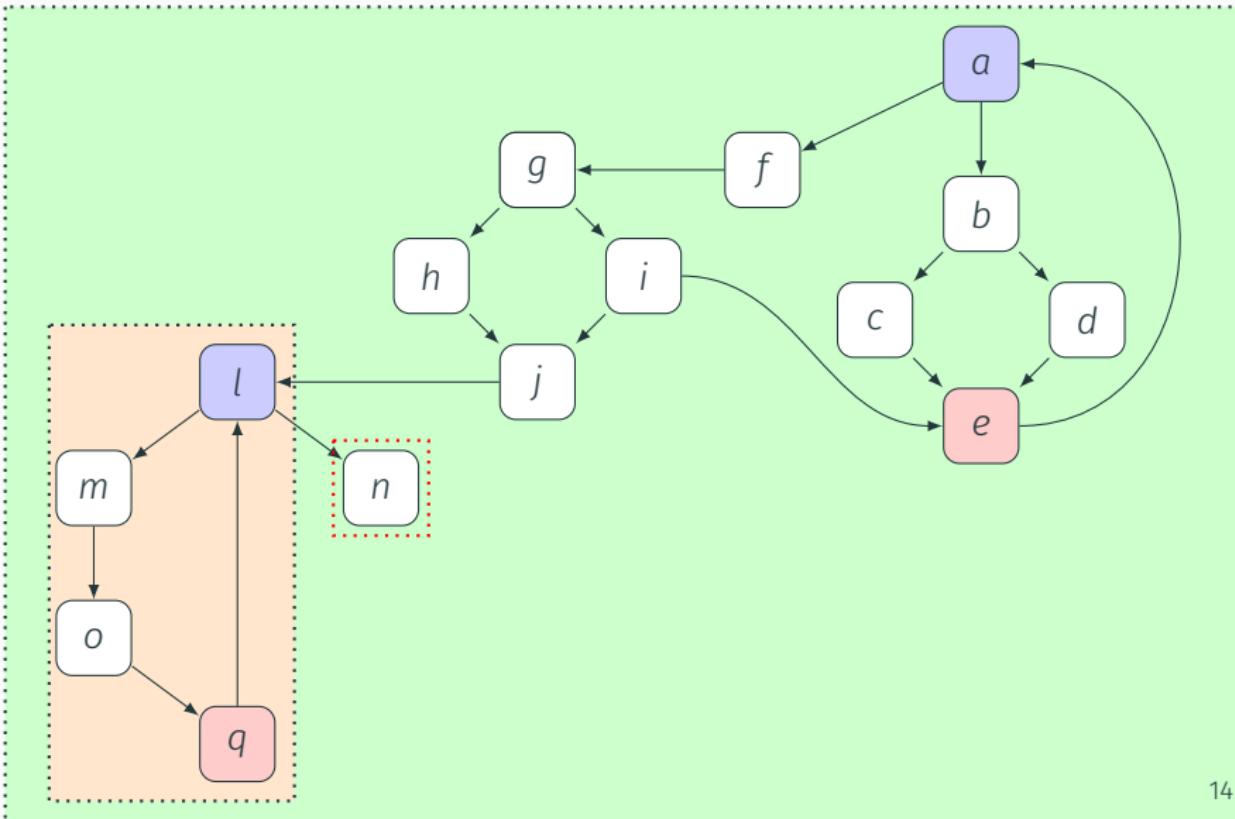
Edge Deletion



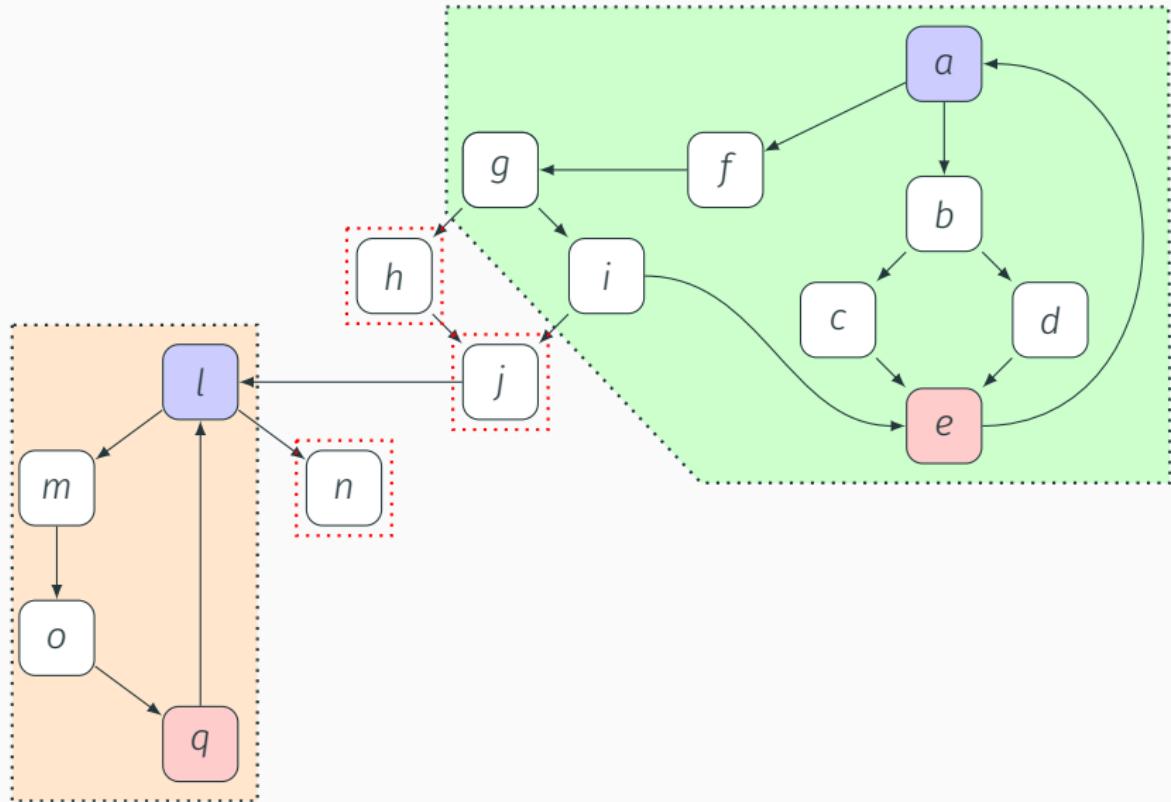
Edge Deletion



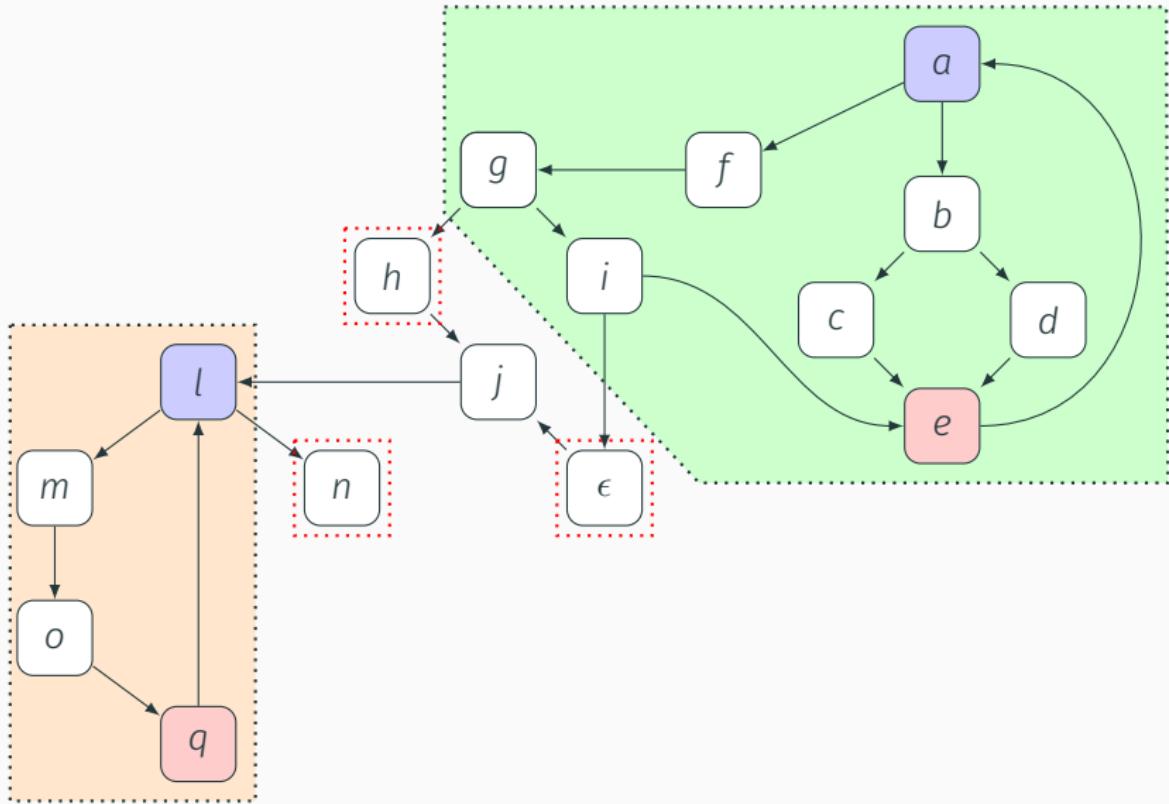
Edge Deletion



Edge Deletion



Edge Deletion



Tasklist

Remaining Work

1. Solidify Current Work
2. CF Preservation on Edge Insertion (e.g. Jump Threading)
3. Implement Bag of Optimizations
4. Evaluation

Questions?